

The structure of the magnetic reconnection exhaust boundary

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What controls the acceleration of the plasma crossing into the reconnection exhaust?

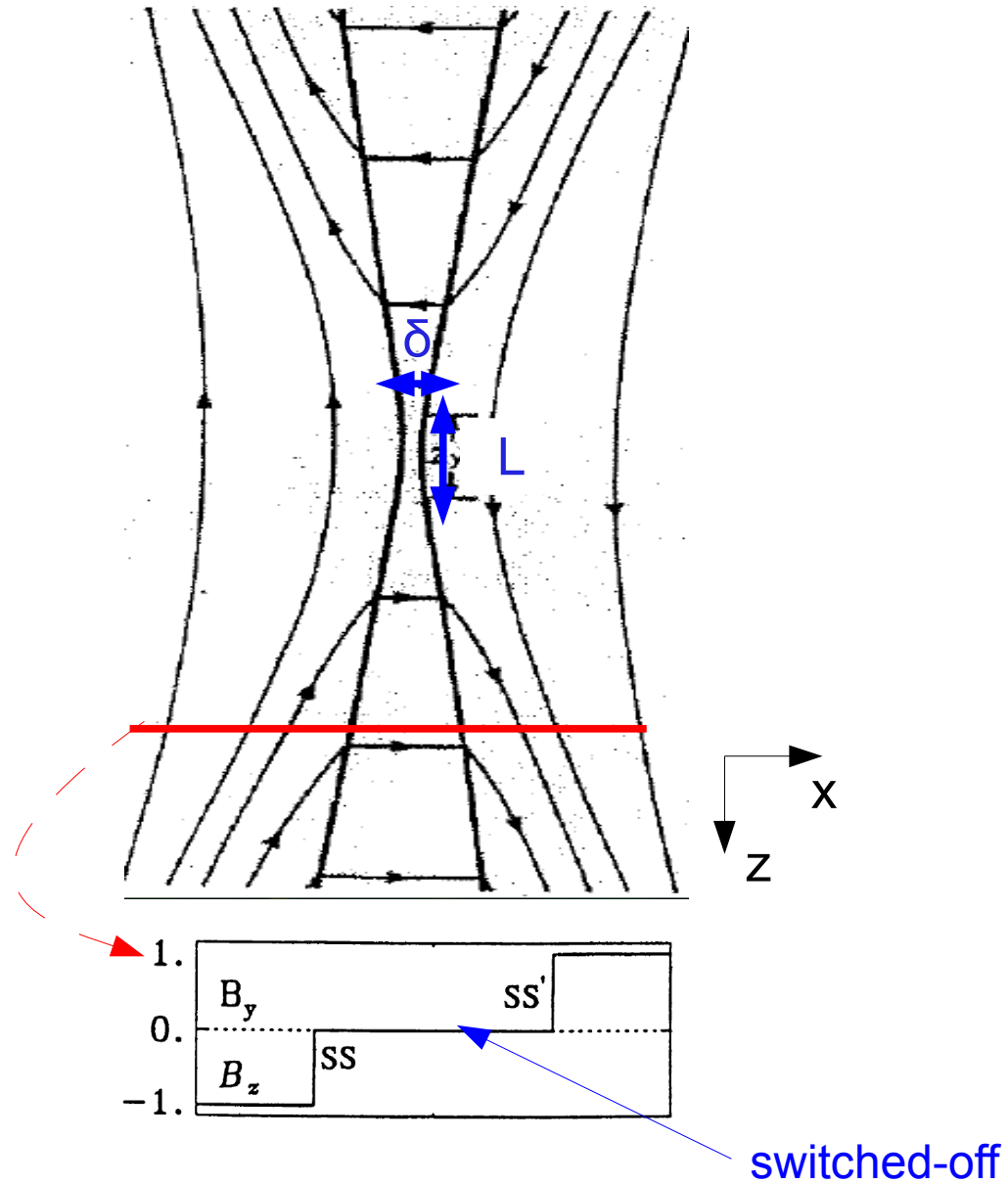
- Standing **Switch-off Slow Shocks** are the key to Petscheck's model.
(Petschek 1964)
- X-ray emissions at solar flares are related to these slow shocks.
(Tsuneta 1996, Longcope & Guidoni 2011)

What happens in collisionless plasmas?

- In-situ observations of **Switch-off Slow Shocks** are rare.
(Seon et al. 1996)
- No **Switch-off Slow Shocks** seen in kinetic reconnection simulations (hybrid & PIC).
(Lottermoser, Scholer & Matthews 1998, Lin & Swift 1996)
- Strong firehose-sense temperature anisotropy ($T_{\parallel} > T_{\perp}$) due to the counter-streaming ions.
(Gosling et al. 2005, Hoshino et al. 1998)

→ Q: if not **Switch-off Slow Shocks**, what is bounding the reconnection exhausts?

Petscheck 101



Structure of the reconnection exhaust

2D PIC simulation, $m_i/m_e=25$

- Petschek-like open exhaust
 - NO Switch-off Slow Shocks
- ϵ weakens the magnetic tension

$$\rho \left(\frac{d\mathbf{V}}{dt} \right)_\perp + \nabla_\perp \left(p_\perp + \frac{B^2}{2\mu_0} \right) = \epsilon \left[\frac{(\mathbf{B} \cdot \nabla)\mathbf{B}}{\mu_0} \right]_\perp$$

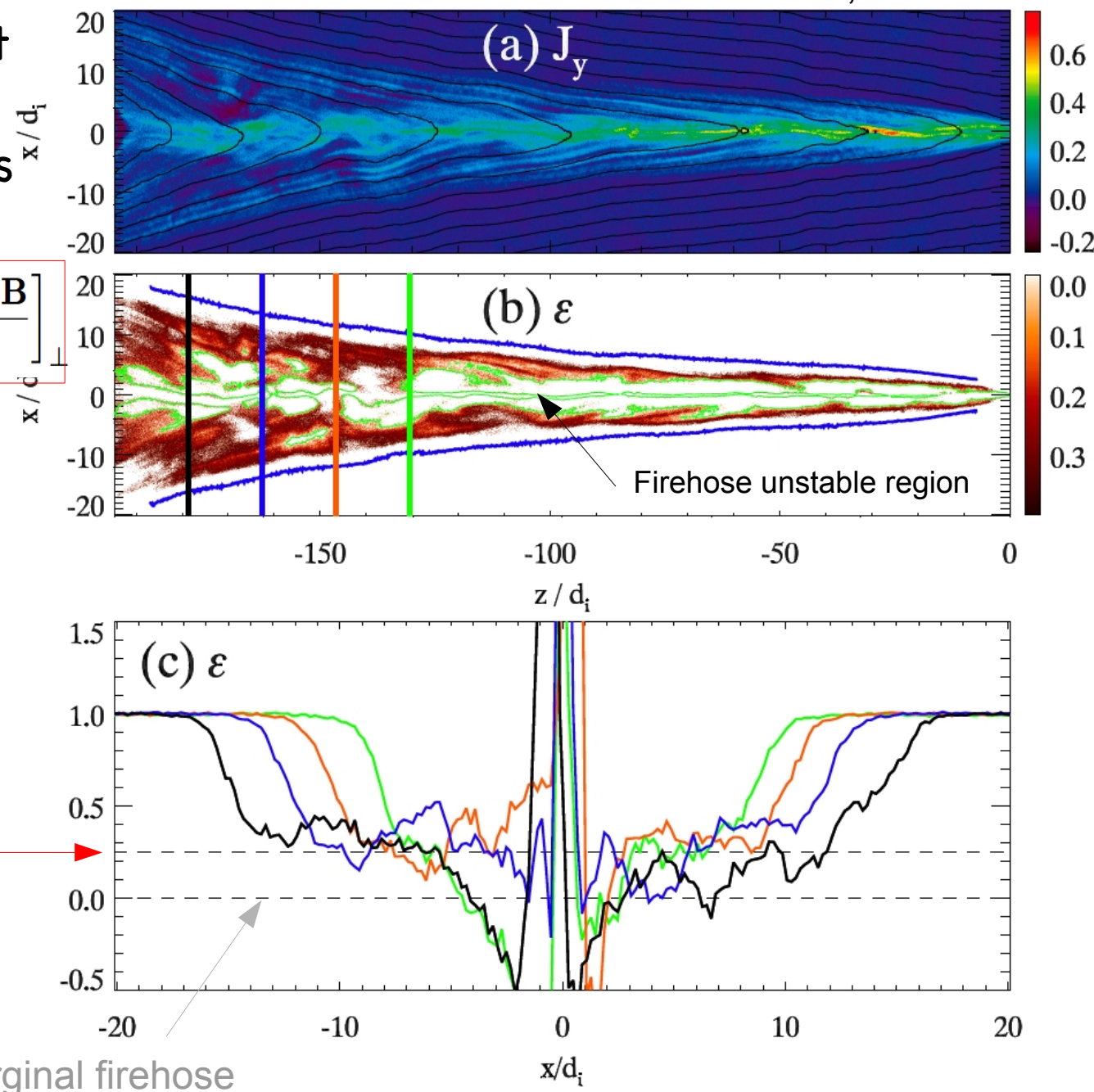
- Firehose unstable near the symmetry line

- Outflow exhibits plateau formation around

$$\epsilon \equiv 1 - \frac{P_\parallel - P_\perp}{B^2/\mu_0} = 0.25$$

WHY??

marginal firehose



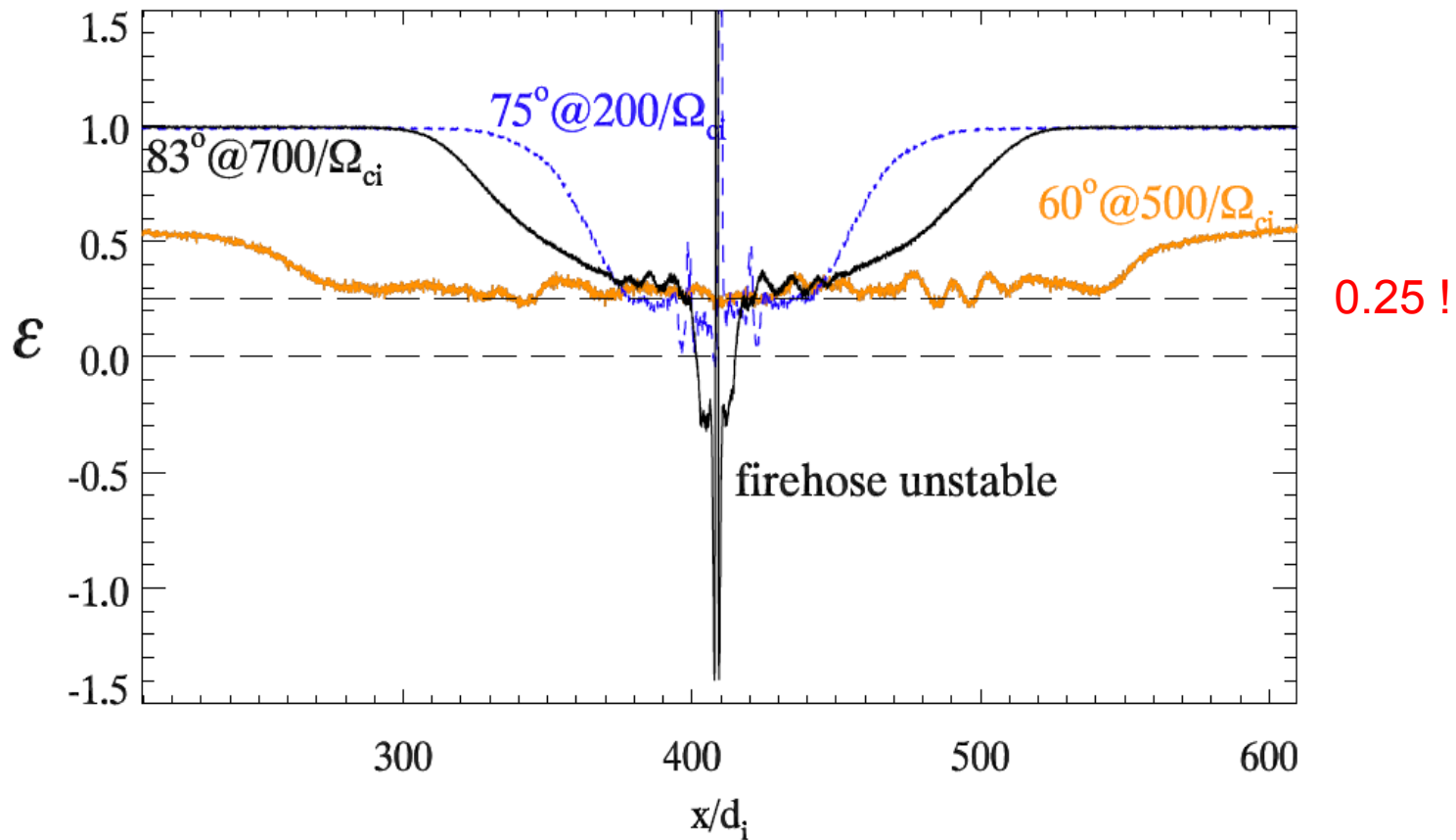
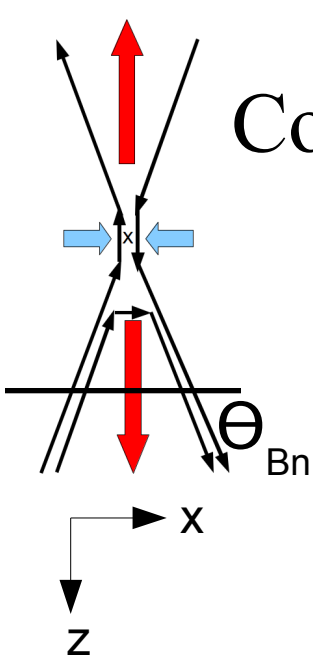
Development of long reconnection exhaust



$m_i/m_e=25$

- Long Petschek-like open exhaust.
- Short (d_i) scale waves are radiated from the center.

Companion Riemann Problems show similar plateaus



- ε plateaus at 0.25 when shock is oblique enough.
- $\varepsilon = 0.25$ is always associated with the onset of rotational waves behind a slow shock! **Why?**

$$\varepsilon \equiv 1 - \frac{P_{\parallel} - P_{\perp}}{B^2/\mu_0}$$

Anisotropic Rankine-Hugoniot Jump Conditions

(Chao 1970, Hudson 1970)

Continuity:

$$[\rho V_x]_d^u = 0$$

Momentum:
(normal)

$$\left[\rho V_x^2 + P + \frac{1}{3} \left(\varepsilon + \frac{1}{2} \right) \frac{B^2}{\mu_0} - \varepsilon \frac{B_x^2}{\mu_0} \right]_d^u = 0$$

Momentum:
(transverse)

$$\left[\rho V_x \mathbf{V}_t - \varepsilon \frac{B_x \mathbf{B}_t}{\mu_0} \right]_d^u = 0$$

Energy:

$$\left[\left(\frac{1}{2} \rho V^2 + \frac{5}{2} P + \frac{1}{3} (\varepsilon - 1) \frac{B^2}{\mu_0} \right) V_x - (\varepsilon - 1) \frac{B_x \mathbf{B}_t}{\mu_0} \cdot \mathbf{V}_t - (\varepsilon - 1) \frac{B_x^2}{\mu_0} V_x + Q_x \right]_d^u = 0$$

Heat flux

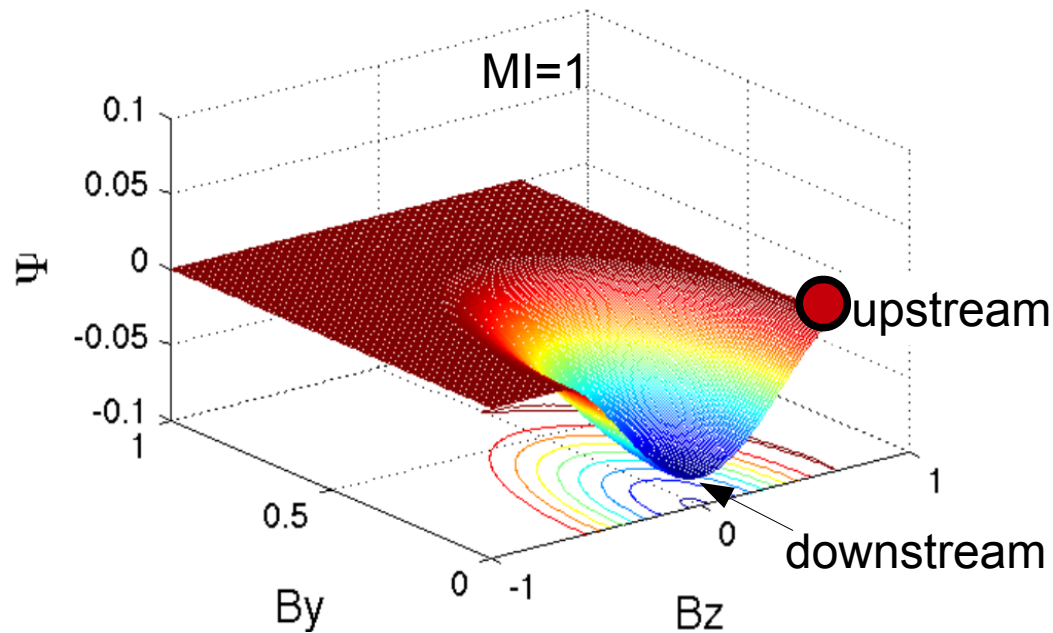
@ DeHoffmann-Teller frame

$$\varepsilon \equiv 1 - \frac{P_{\parallel} - P_{\perp}}{B^2 / \mu_0}$$

The analysis of shock Pseudo-Potential

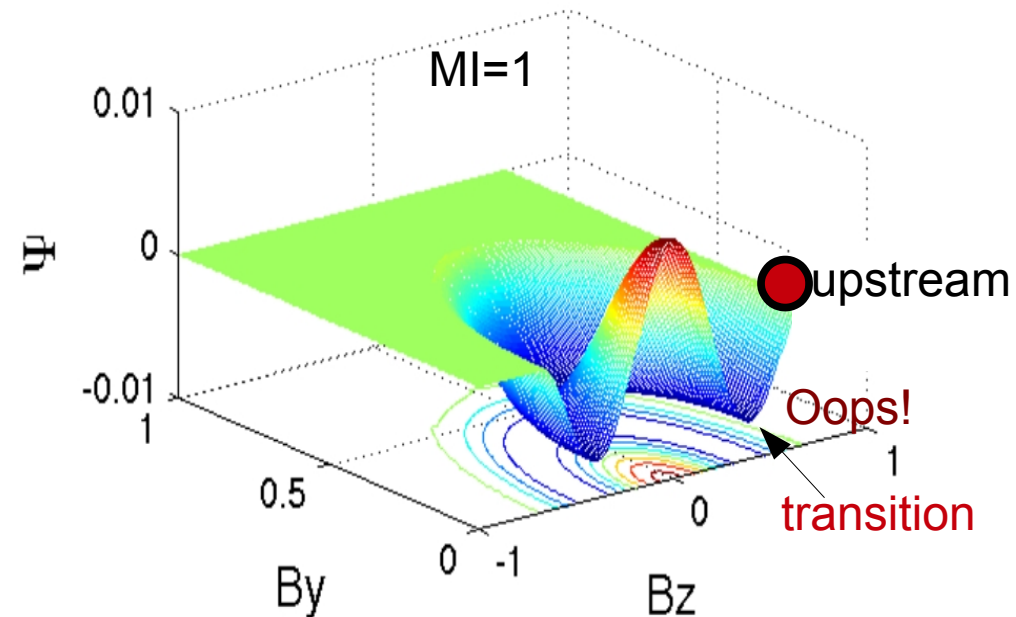
(From Switch-off Slow Shocks to compound SS/RD waves)

Isotropic fluid theory



→ Switch-off Slow Shock (SSS)

Anisotropic fluid theory
(when anisotropy is strong enough...)

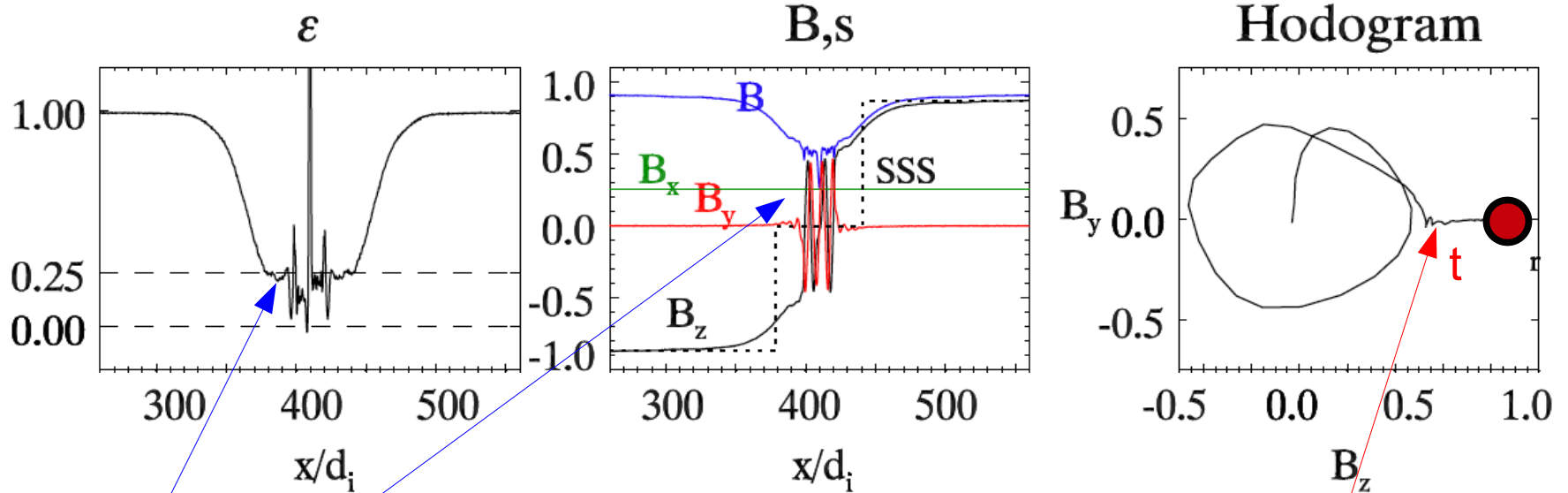
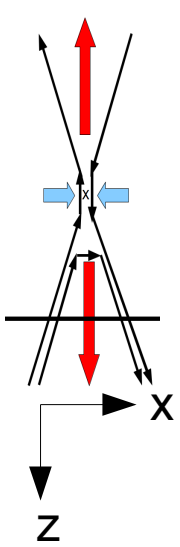


→ compound SS/RD wave

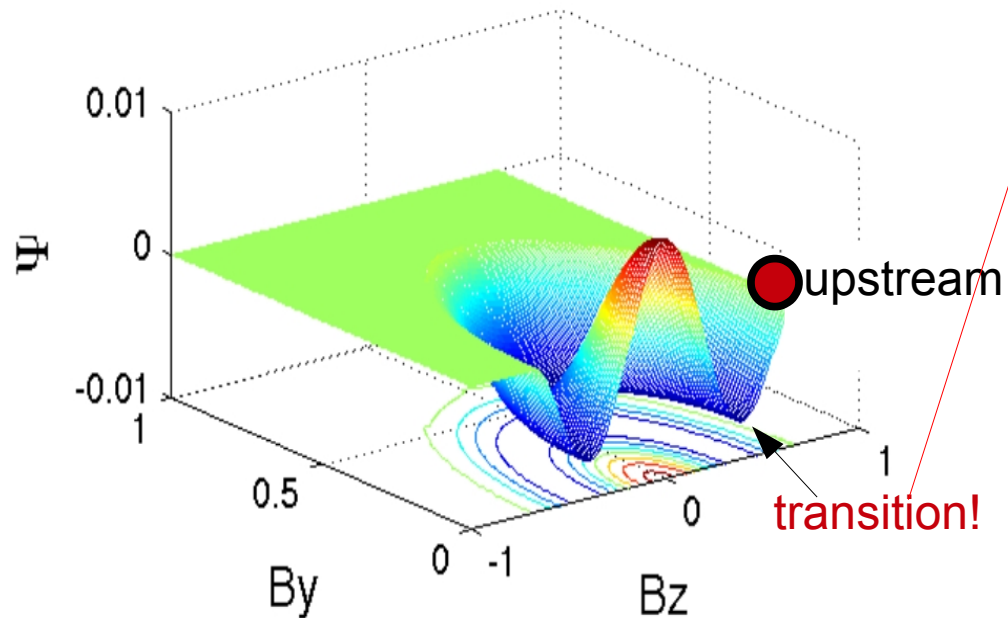
- Pseudo-particle cannot access to the origin and cannot form SSS
→ Instead, a **compound Slow/Intermediate wave forms.**
- Underline physics: intermediate mode becomes slower than slow mode.
→ Linear modes analysis: Abrham-Shrauner 1967; Hau & Sonnerup 1993; Walthour et al. 1997

Compare with simulation

Companion 1D Riemann Problem



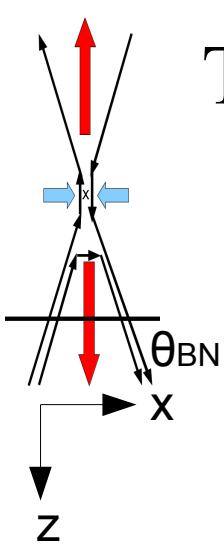
Onset of rotational mode



- Similar coplanar to non-coplanar transition is seen!

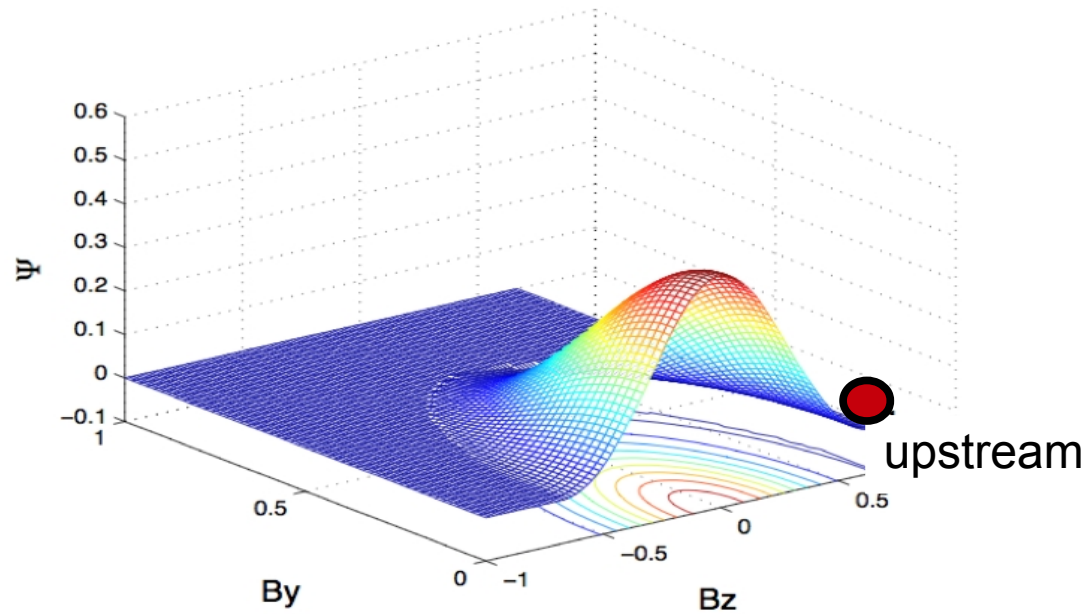
$$\varepsilon \equiv 1 - \frac{P_{\parallel} - P_{\perp}}{B^2/\mu_0}$$

The significance of 0.25 in anisotropic fluid theory



$$\epsilon_0 < 0.25$$

$$\epsilon \equiv 1 - \frac{P_{\parallel} - P_{\perp}}{B^2/\mu_0}$$



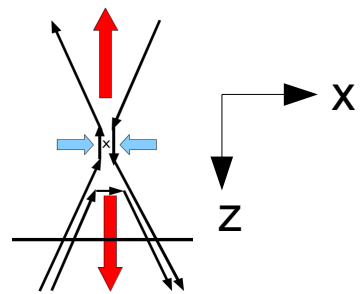
$\gamma=5/3$ for monatomic plasmas

From a simplified equation

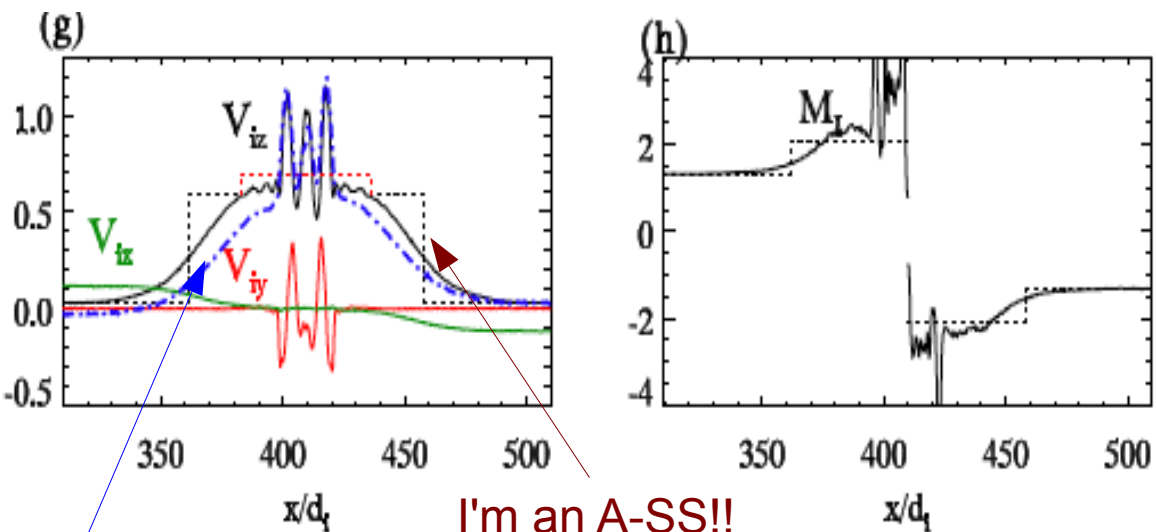
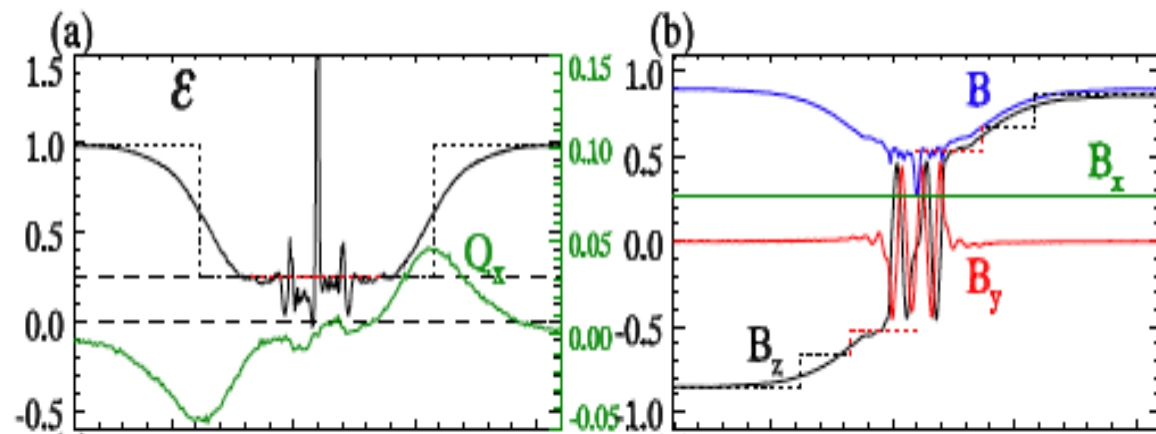
- If $\epsilon_0 < (3\gamma-4)/(3\gamma-1) = 0.25$,
- nonlinearity " $\alpha \sim (3\gamma-1)\epsilon_0 - (3\gamma-4)$ " changes sign
- Slow mode becomes fast-mode-like.
- there is no slow mode transition!
- $\epsilon = 0.25$ is an "absolute" barrier that a SSS cannot cross.
- In the oblique limit, a general critical ϵ that a SSS cannot reach,

Independent of β_u , ϵ_u & θ_{BN}

$$\epsilon_{cr} = \frac{-2\epsilon_u^2 + (15\beta_u + 8)\epsilon_u}{10\epsilon_u + 15\beta_u + 5}$$



Rankine-Hugoniot Jumps vs. 1D Riemann structure

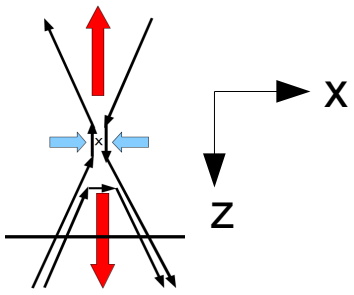


Walén test
(Sonnerup et al. 1981)

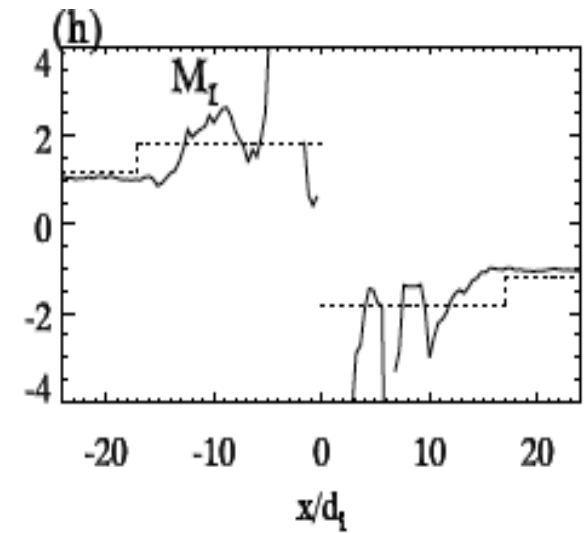
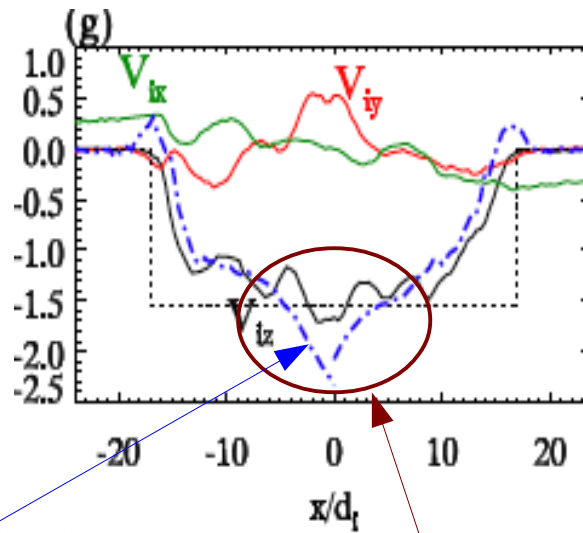
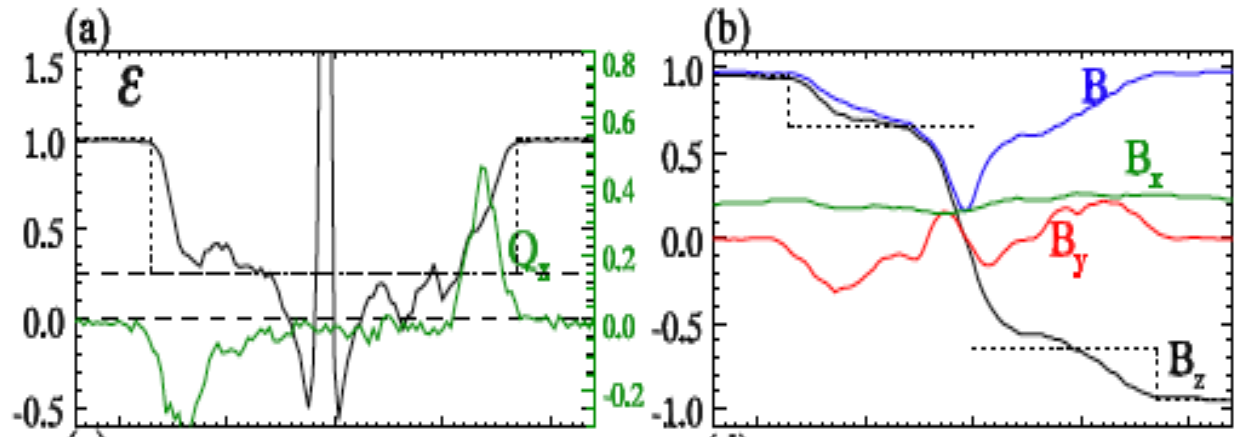
$$\varepsilon \equiv 1 - \frac{P_{\parallel} - P_{\perp}}{B^2/\mu_0}$$

- Slow shock upstream
→ Super intermediate to super intermediate transition !!
(super slow to sub slow)
→ **Anomalous slow shock (A-SS).**
(Karimabadi et al 1995)
→ Dotted lines are the predicted jumps of A-SS.
- Transition to a left-hand (LH) rotational wave downstream at $\varepsilon = 0.25$

Rankine-Hugoniot Jumps vs. reconnection exhaust structure



- The Walen test over predicts the outflow velocity by about 40% .
- **Walen test fails at $\varepsilon < 0$.**
- which is the firehose unstable Regime.
- most outflow driven by A-SS
- Downstream LH rotational wave has not developed well yet.

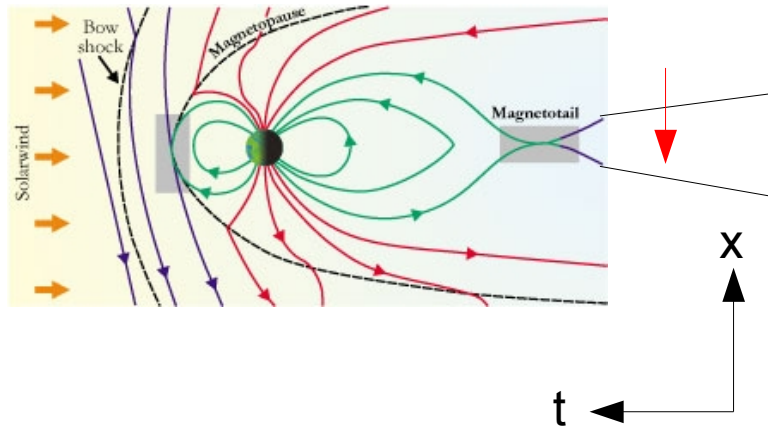


Walen test

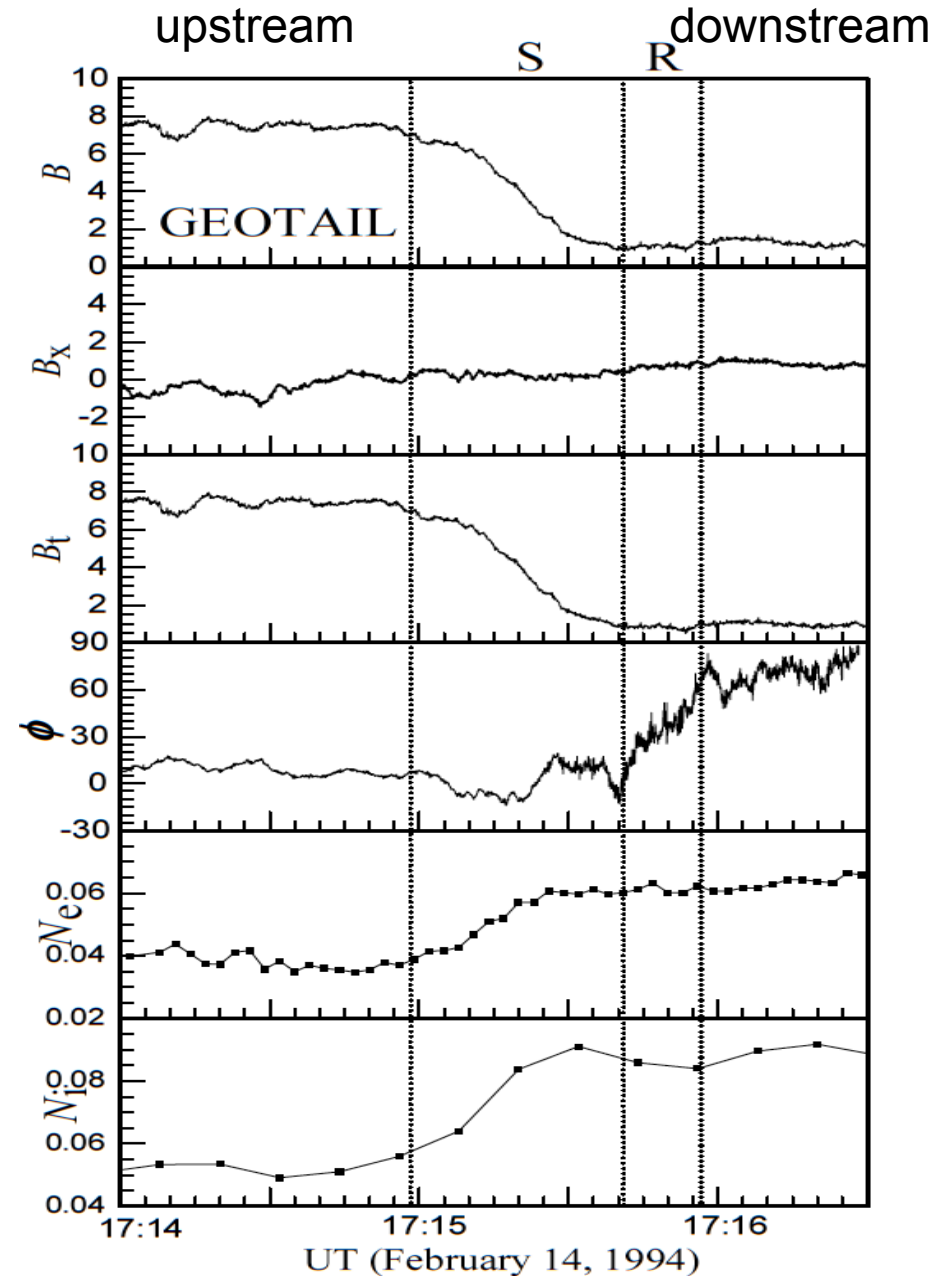
FAIL!!

$$\varepsilon \equiv 1 - \frac{P_{\parallel} - P_{\perp}}{B^2/\mu_0}$$

Observation: Reconnection exhaust crossing

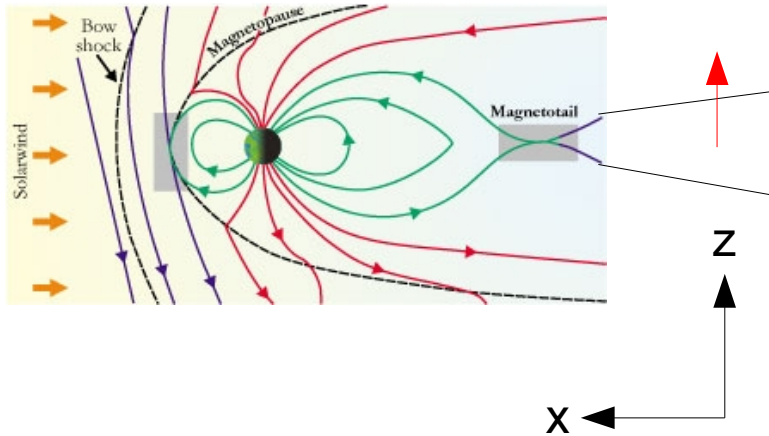


- High temporal resolution.
(60 millisecond VS. 3 seconds)
- LH polarized.
- It was called a “Double Discontinuity”
- Evidence of compound Slow/Intermediate waves?

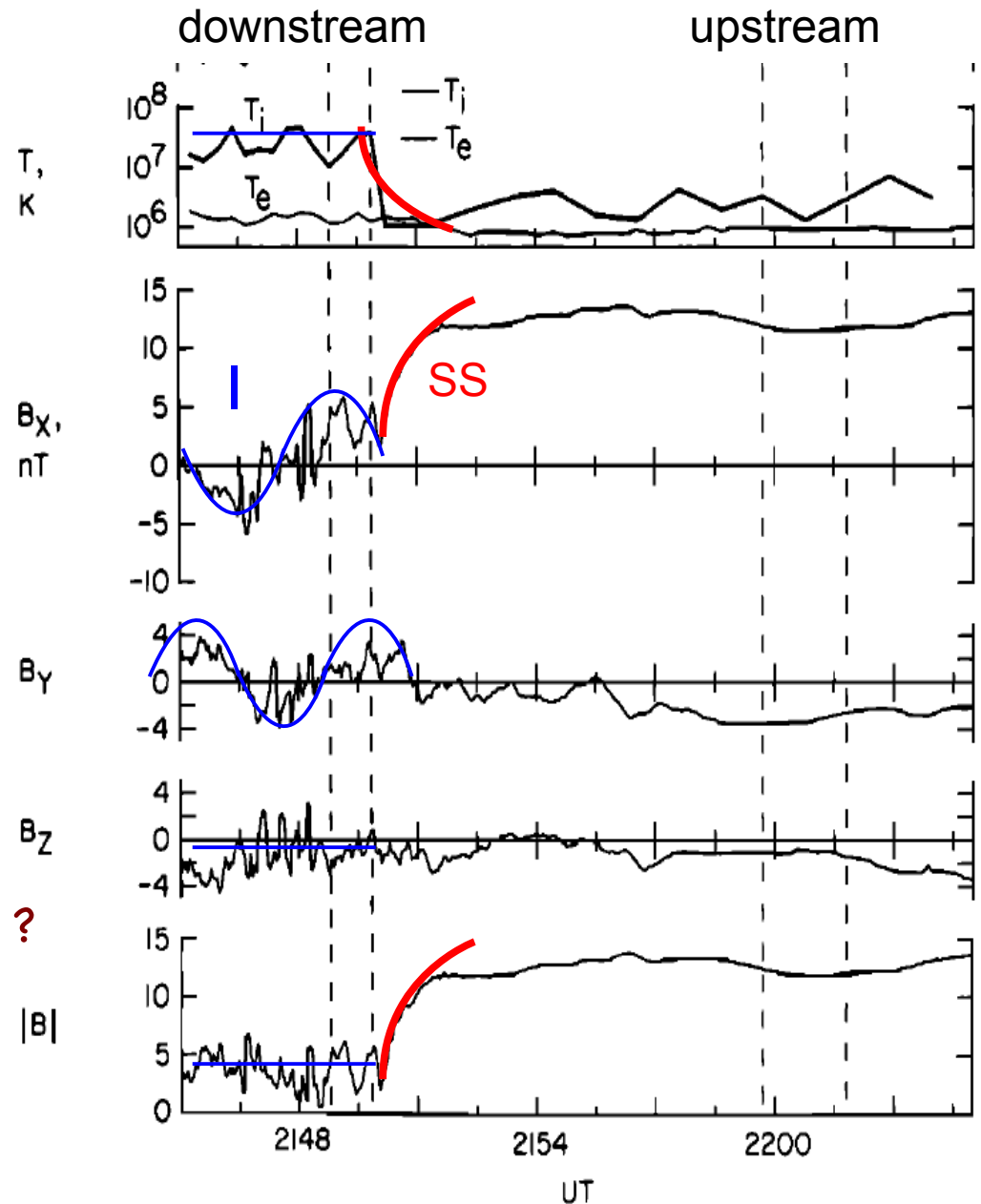


GEOTAIL @ $X_{GSM} = -54R_E$. (Whang, 2004)

Observation: Reconnection exhaust crossing- 2



- LH polarized.
- Evidence of compound Slow/Intermediate waves ?



GEOTAIL @ $X_{GSM} = -181.8 R_E$. (Seon et al. 1996)

Summary

- $\epsilon = 0.25$ plateau forms at reconnection exhaust boundary.
- $\epsilon = 0.25$ is a special point in RH jump conditions.
 - It is closely related to the degenerate behavior of slow & intermediate modes due to the temperature anisotropy.
- Switch-off Slow Shocks cannot transition to $\epsilon < 0.25$,
 - therefore Petschek's Switch-off Slow Shocks cannot be realized.
 - this explains the rareness of SSSs in space.
 - Overall, a compound Anomalous Slow Shock/Intermediate wave forms.
- The reconnection outflow speed is usually slower than expected.
 - due to the firehose unstable region
 - reconnection outflow is driven by A-SS
- $\epsilon = 0.25$ should be an **in-situ observable signature** in tail reconnection.

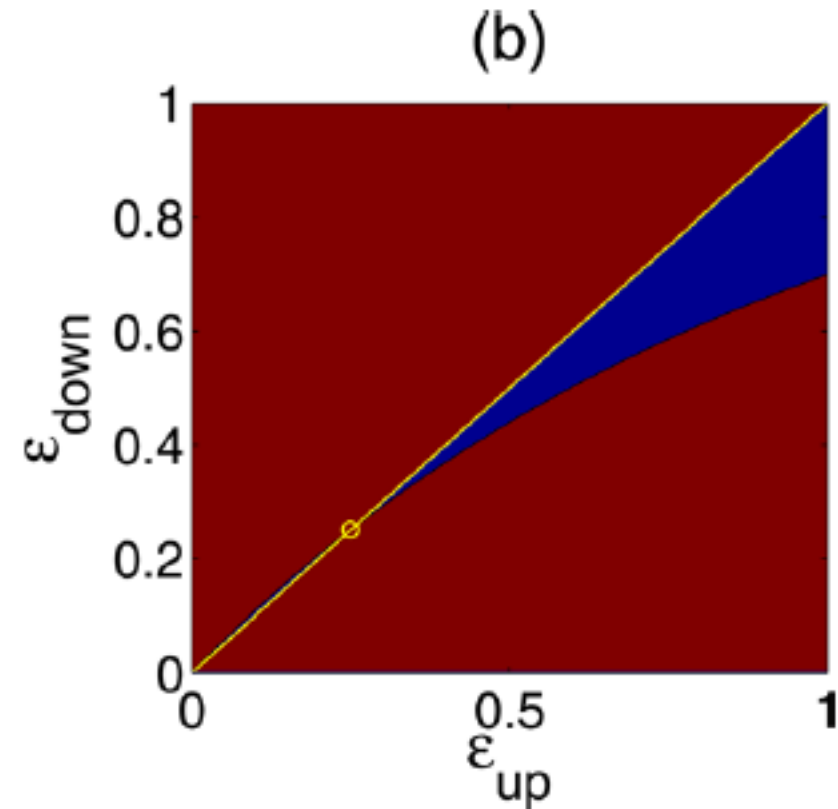
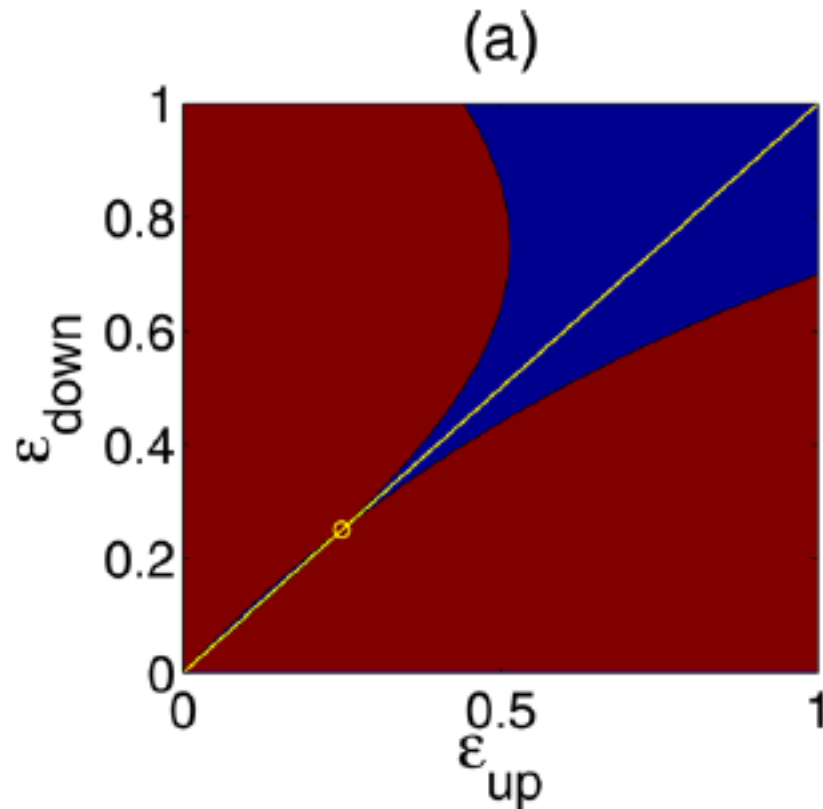


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Anisotropic Rotational Discontinuity

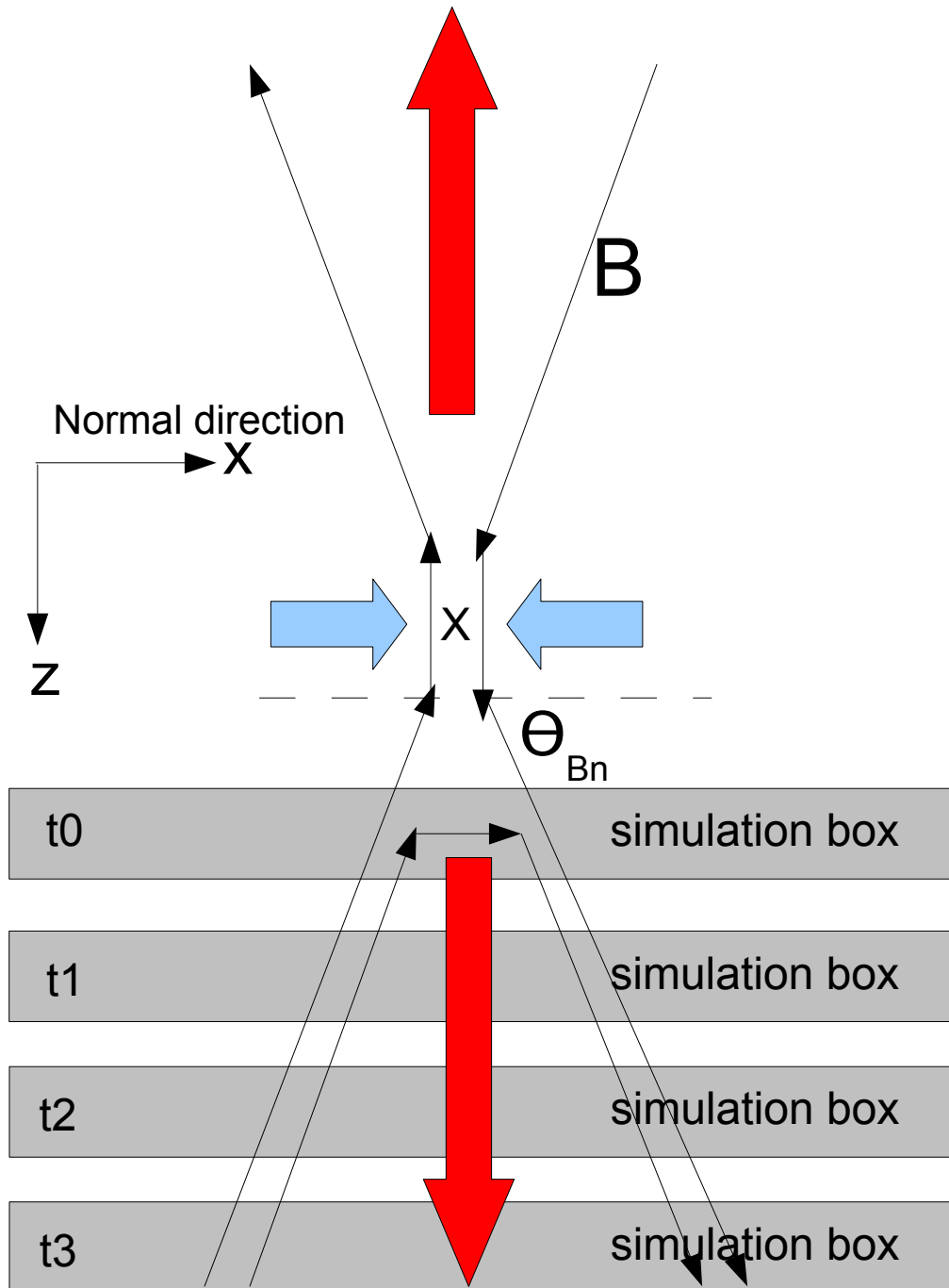
(Hudson 1970)

Consider entropy condition



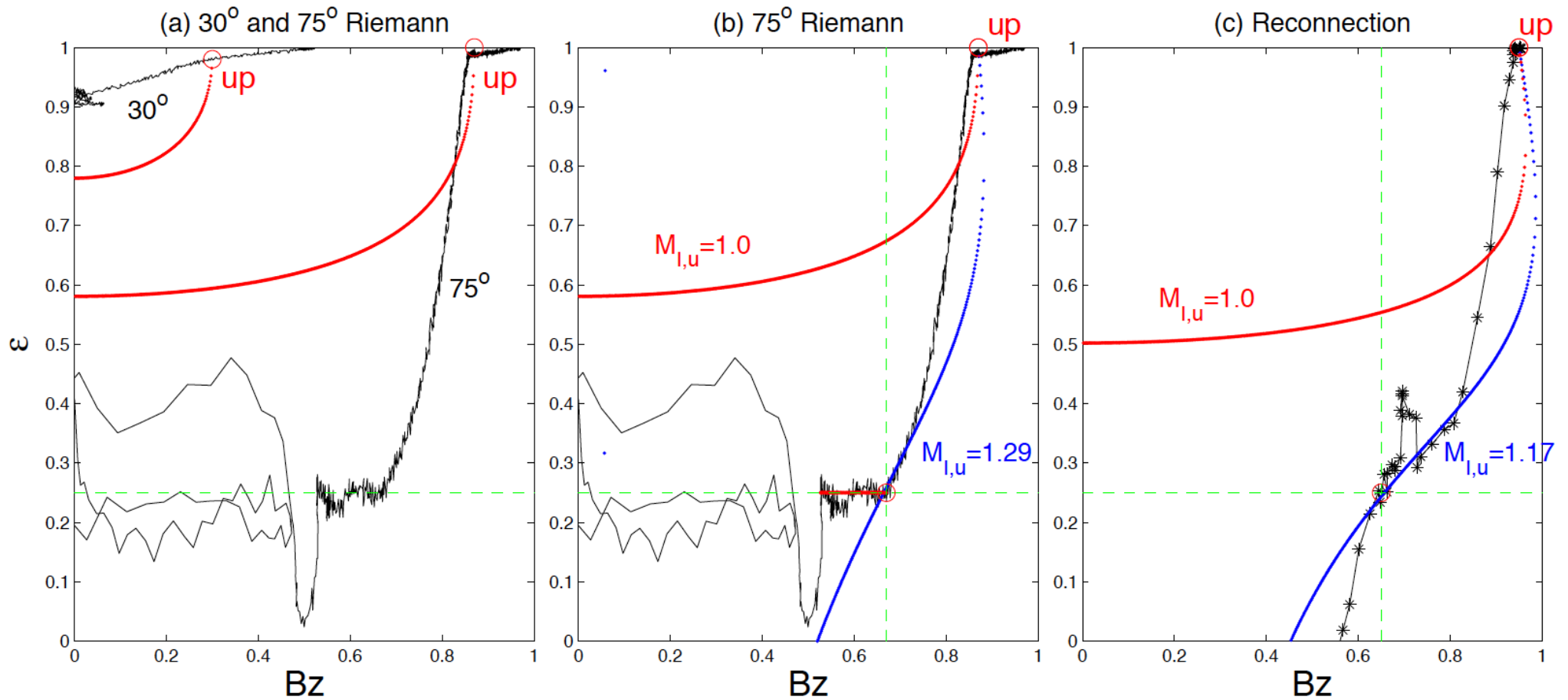
- Hudson thinks although 0.25 is special, but not important in space.
- Out of Hudson's surprise,
 - We find a place to reveal the specialty of 0.25.
 - it is inside the reconnection exhaust!!

The setup of our PIC Riemann simulations



- Initial profile:
Harris Sheet [$B_z = B_0 \tanh(x/w)$] + B_x
- Driven by the unbalanced magnetic tension force.
- It is a Riemann problem.
(Scholer & Lottermoser et al. 1998,
Lin & Lee et al. 1993)
- Use time as a proxy of space
- A much longer domain in the normal direction. (~ 800 di)
- θ_{BN} is one of the key parameters that controls the propagation angle.

The way of determining the Mach number

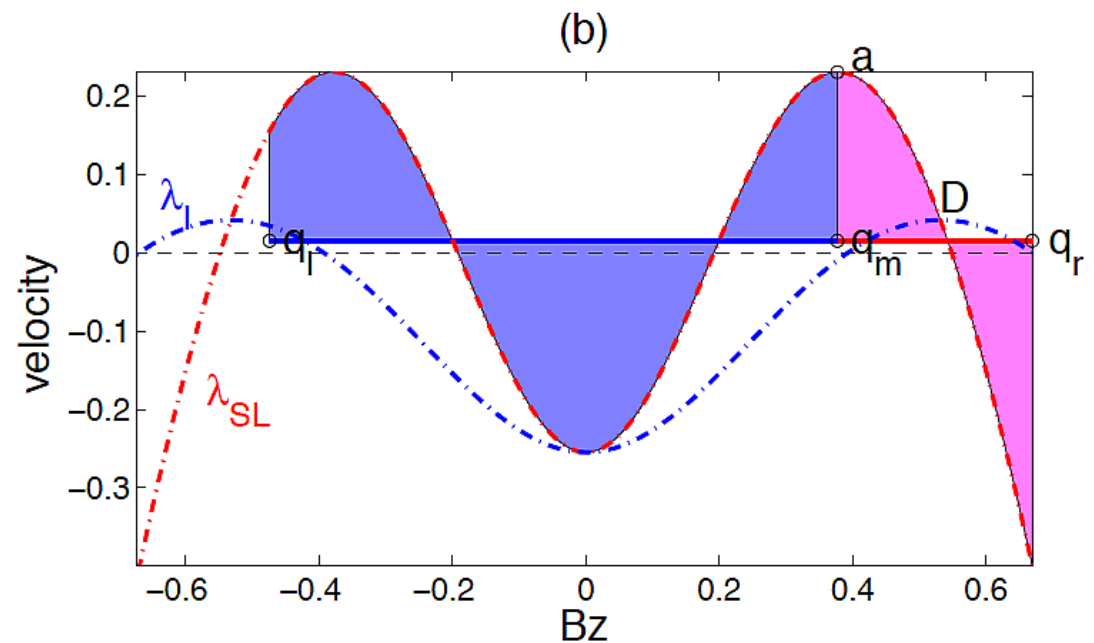
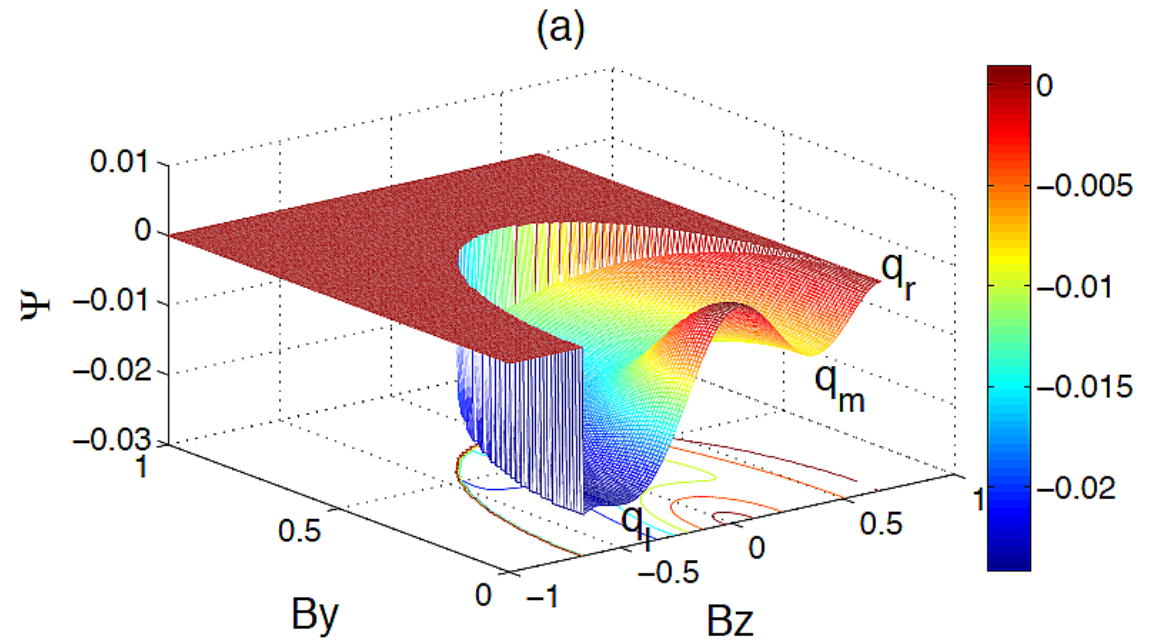


→ Increase $M_{l,u}$ till the SS solution curve intersects with the data curve at $\varepsilon = 0.25$

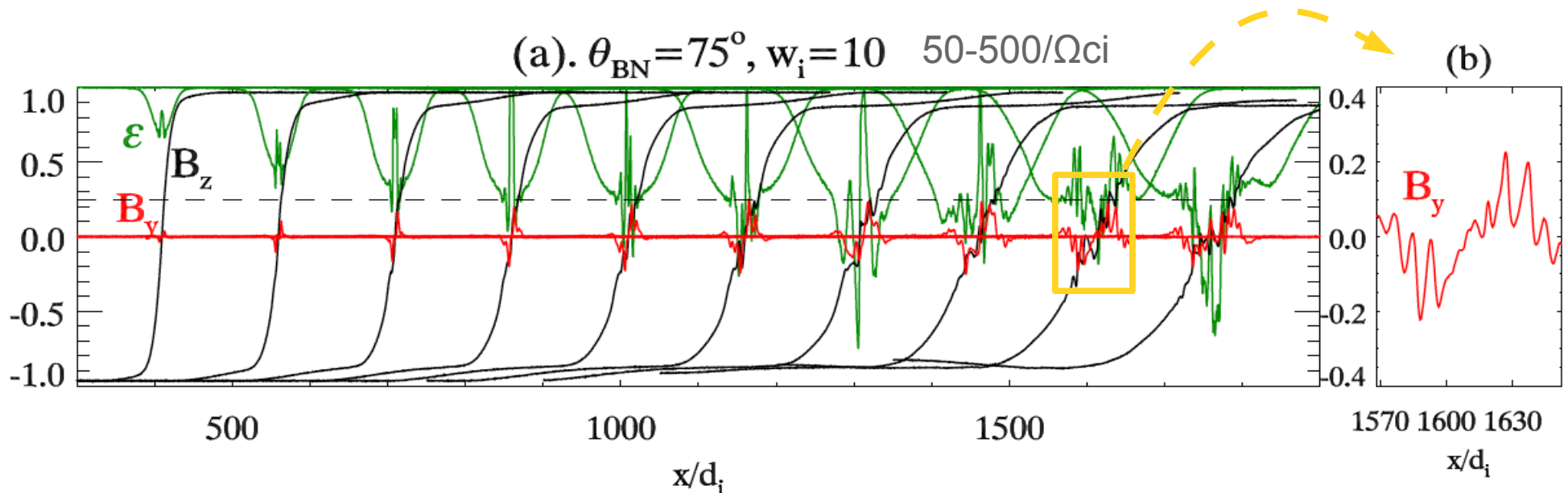
Being slightly super-intermediate...

- The analysis of slow and intermediate characteristics shows the formation of compound A-SS/IS wave

(Liu et al 2011)

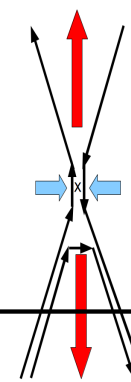


The rotational part of the SS/RD is not stable!



- The rotational part of SS/RD tends to break into ion inertial scale waves!
→ spatially modulated rotational wave radiates dispersive waves.
- ϵ is raised by scattering from these di-scale waves.

$$\epsilon \equiv 1 - \frac{P_{\parallel} - P_{\perp}}{B^2/\mu_0}$$



Anisotropic Derivative NonLinear Schrodinger-Burgers equation

Extend the work of Kennel et al. 1990

$$\partial_\tau \mathbf{b}_t + \partial_\eta [\alpha \mathbf{b}_t (b_t^2 - b_{t0}^2) + \Omega \mathbf{b}_t (\varepsilon - \varepsilon_0)] = \partial_\eta (R \partial_\eta \mathbf{b}_t) - \frac{1}{2\sqrt{\varepsilon_0}} d_i \partial_\eta^2 (\hat{\mathbf{e}}_x \times \mathbf{b}_t)$$

Nonlinear steepening

Dissipation

Dispersion

$$\alpha \propto (3\gamma - 1)\varepsilon_0 - (3\gamma - 4)$$

\mathbf{b}_t : transverse magnetic field

The difference between the slow and intermediate characteristic speeds is:

$$\lambda_{SL} - \lambda_I = 2\alpha b_t^2 + \Omega \delta\varepsilon_{b_t} b_t$$

Therefore, the slow and intermediate modes degenerate (i.e., **have the same speed**) at:

$$b_t = 0.$$

The traditional degeneracy point

$$2\alpha b_t + \Omega \delta\varepsilon_{b_t} = 0$$

← **New degeneracy points due to the temperature anisotropy!!**

$$\varepsilon \equiv 1 - \frac{P_{\parallel} - P_{\perp}}{B^2/\mu_0}$$

Calculate the pseudo-potential (Sagdeev potential)

Looking for stationary solutions: $\mathbf{b}_t = \mathbf{b}_t[\xi(\eta - V_S\tau)]$
 Shock speed

$$\int \dots d\xi$$

$\xi \rightarrow$ time

$\tau \rightarrow$ spatial coordinate

$$\rightarrow R\partial_\xi \mathbf{b}_t - \frac{1}{2\sqrt{\epsilon_0}} d_i \partial_\xi (\hat{\mathbf{e}}_x \times \mathbf{b}_t) = -V_S(\mathbf{b}_t - \mathbf{b}_{t0}) + \alpha_{\text{eff}}(b_t) \mathbf{b}_t (b_t^2 - b_{t0}^2) \equiv \partial_{\mathbf{b}_t} \Psi(b_y, b_z)$$

Friction Coriolis force Nonlinear term Potential gradient force

$$\int (\dots) \cdot \partial_\xi \mathbf{b}_t d\xi$$

$$\rightarrow \Psi|_{\text{up}}^{\text{down}} = R \int_{\text{up}}^{\text{down}} (\partial_\xi \mathbf{b}_t)^2 d\xi < 0$$

- The pseudo-potential characterizes the **nonlinearity** of this wave system.
- Resistivity sinks pseudo-particles to the potential low \rightarrow shock transition