

# Wind turbine wake characterization with optical remote sensing and computational fluid dynamics

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- Other collaborators
  - Branko Kosović (NCAR)
  - Jeff Mirocha (LLNL)
  - Yelena Pichugina (NOAA)
  - Andy Clifton (NREL)

# Outline

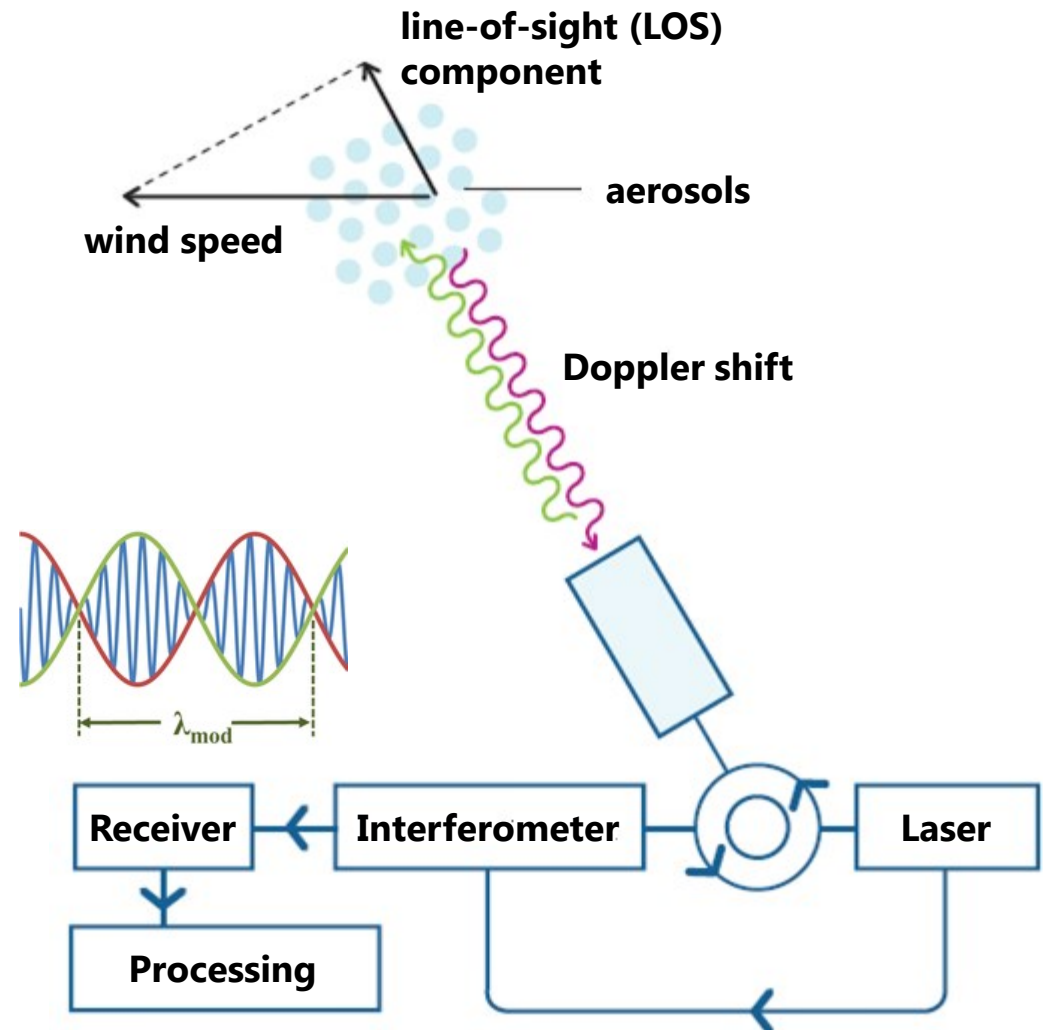
- Lidar background
- Wind turbine wake characterization
  - theory and previous work
  - wake detection algorithm
  - experiment
  - simulation
- Summary

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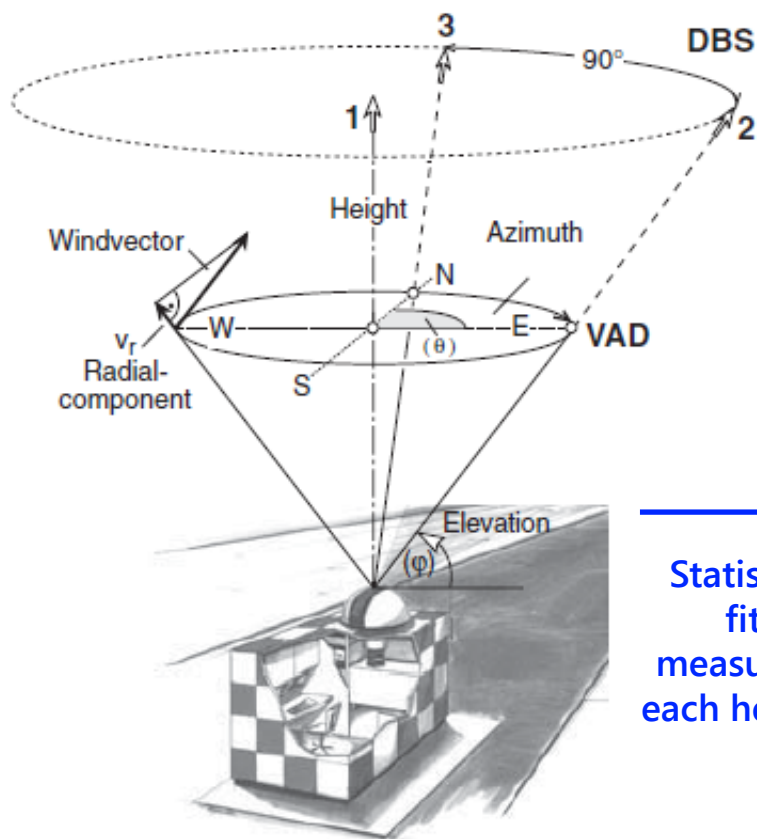
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# Pulsed coherent lidar principle of operation

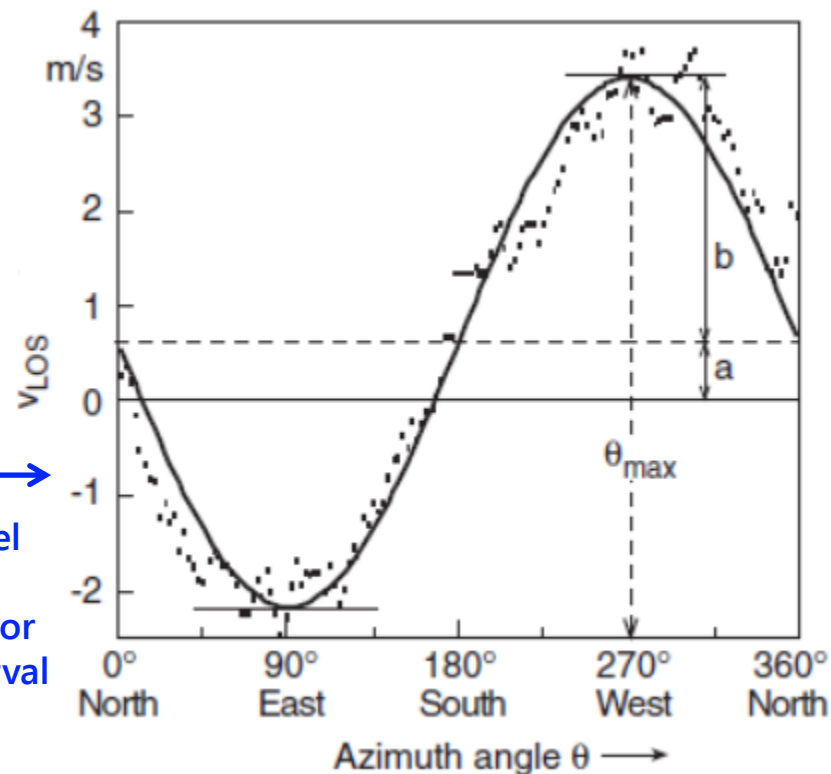
- Transmitted optical signal is scattered from atmospheric aerosols advected by wind
- Return signal optically mixed w/ local oscillator
- Resulting beat frequency indicates Doppler shift due to moving particles
  - wind speed is proportional to Doppler shift
  - offset frequency added to local oscillator to distinguish between (+) and (-) velocities
- Only line-of-sight velocity can be discerned



# Lidar measurements taken usually under the assumption that the flow is homogeneous



Statistical model  
fit to lidar  
measurements for  
each height interval



$$v_{\text{LOS}} = -u \sin \theta \cos \phi - v \cos \theta \cos \phi - w \sin \phi$$

$$v_{\text{LOS}} = a + b \cos(\theta - \theta_{\text{max}})$$

$$\mathbf{v} = (u, v, w) = (-b \sin \theta_{\text{max}} / \cos \phi, -b \cos \theta_{\text{max}} / \cos \phi, -a / \sin \phi)$$

# Lidar applications to wind energy

- Data assimilation for improved forecasting
- Nacelle-based turbine control systems
  - increase energy output
  - decrease structural damage
- Resource assessment
  - reduce uncertainty in annual energy production (AEP)
  - lower borrowing costs
  - improve return on investment (ROI)
- **Wind turbine wake characterization**
  - CFD model verification

Fig: Alfred Wegener Institute



Fig: FT Technologies

Fig: Pentalum

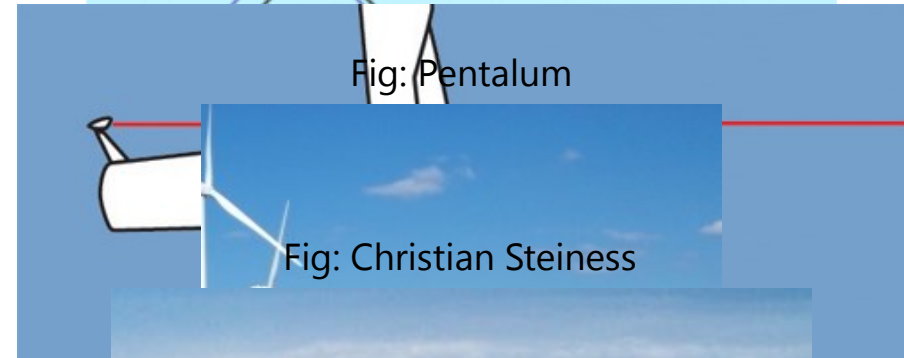


Fig: Christian Steiness

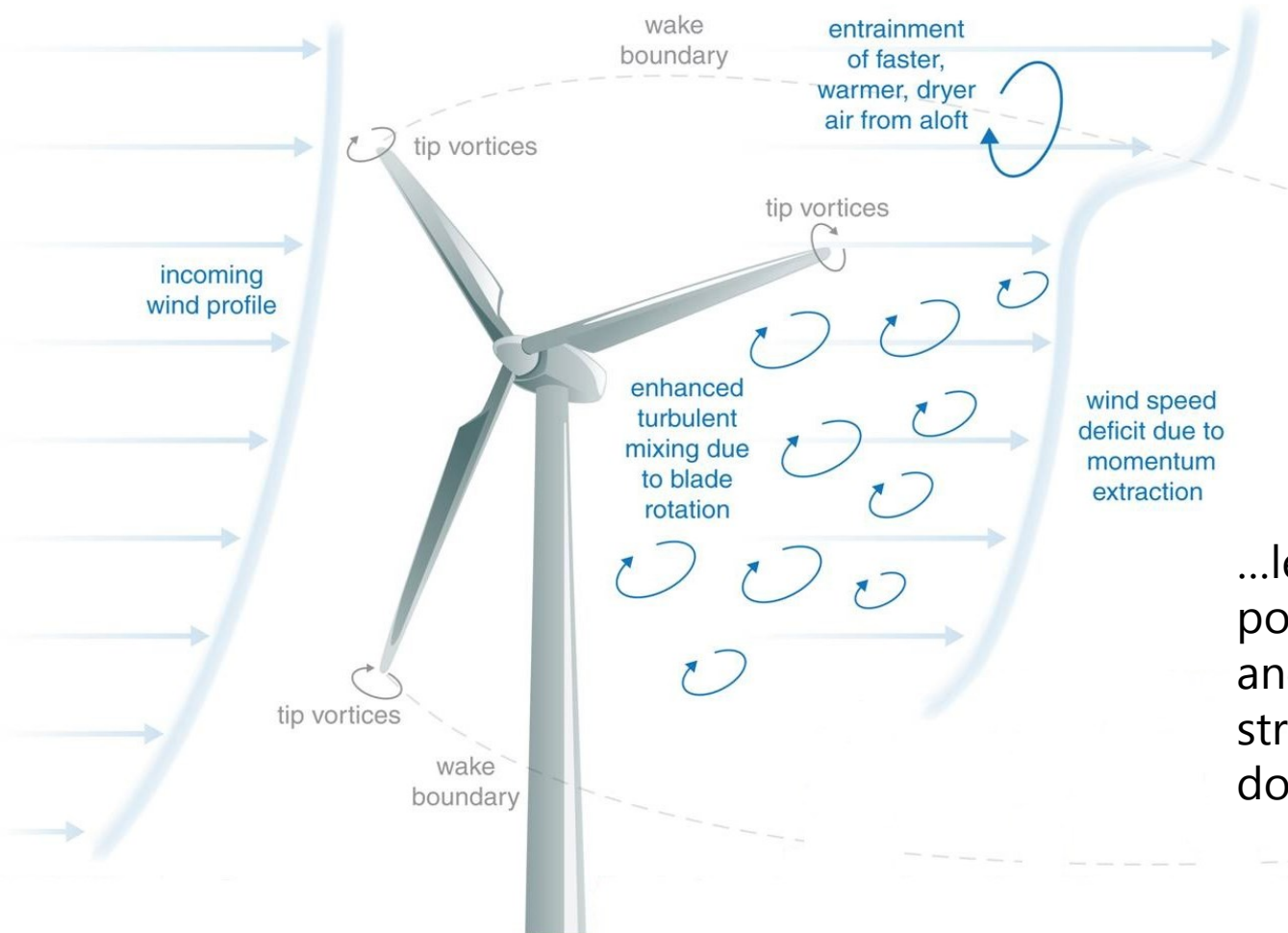


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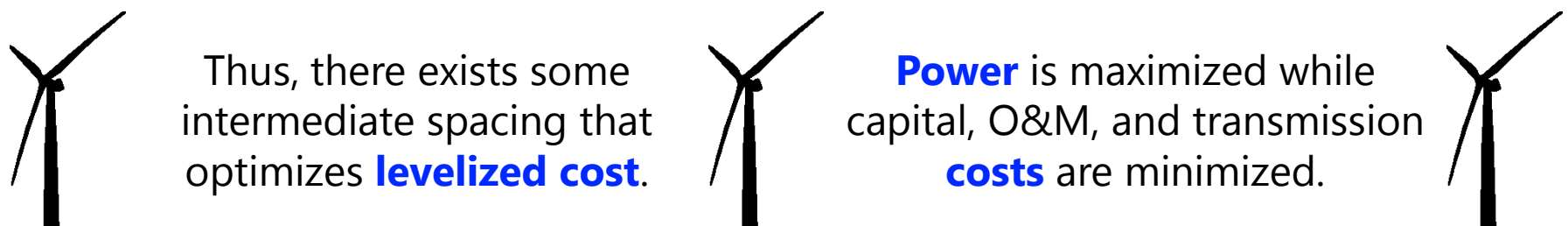
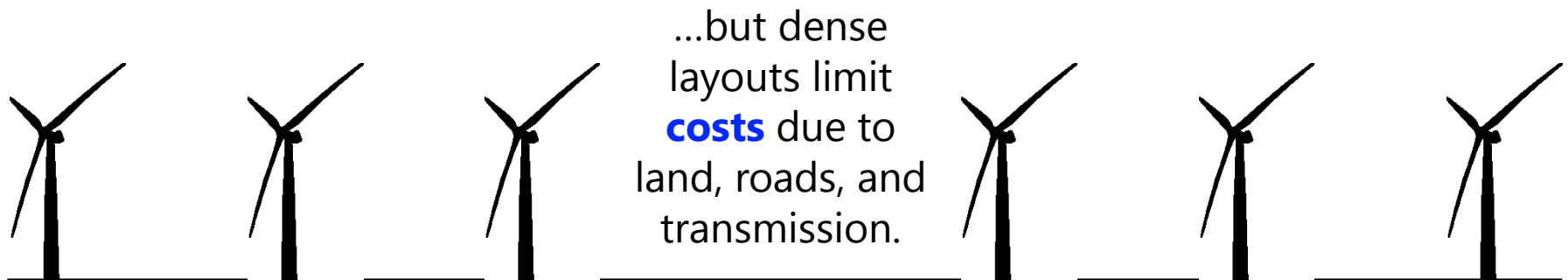
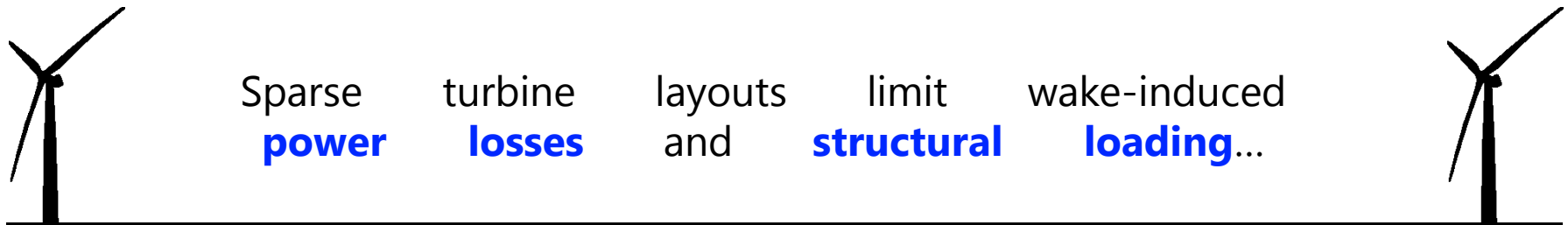


# Wind turbine wakes are characterized by (1) velocity deficit & (2) increased turbulence...



...leading to (1) lower power performance and (2) higher structural loading for downwind turbines

# Motivation: to optimize turbine layouts and controls at wind farms



# Wind turbine layout optimization

- Wind turbine wake modeling suffers from too much uncertainty
  - negatively impacts optimization of wind farm layouts
  - more experimental data needed for model verification
- Innovation in measurement techniques is increasingly important
  - scanning remote sensors offer fine resolution w/o disturbing flow
  - new methods are required to extract wake characteristics

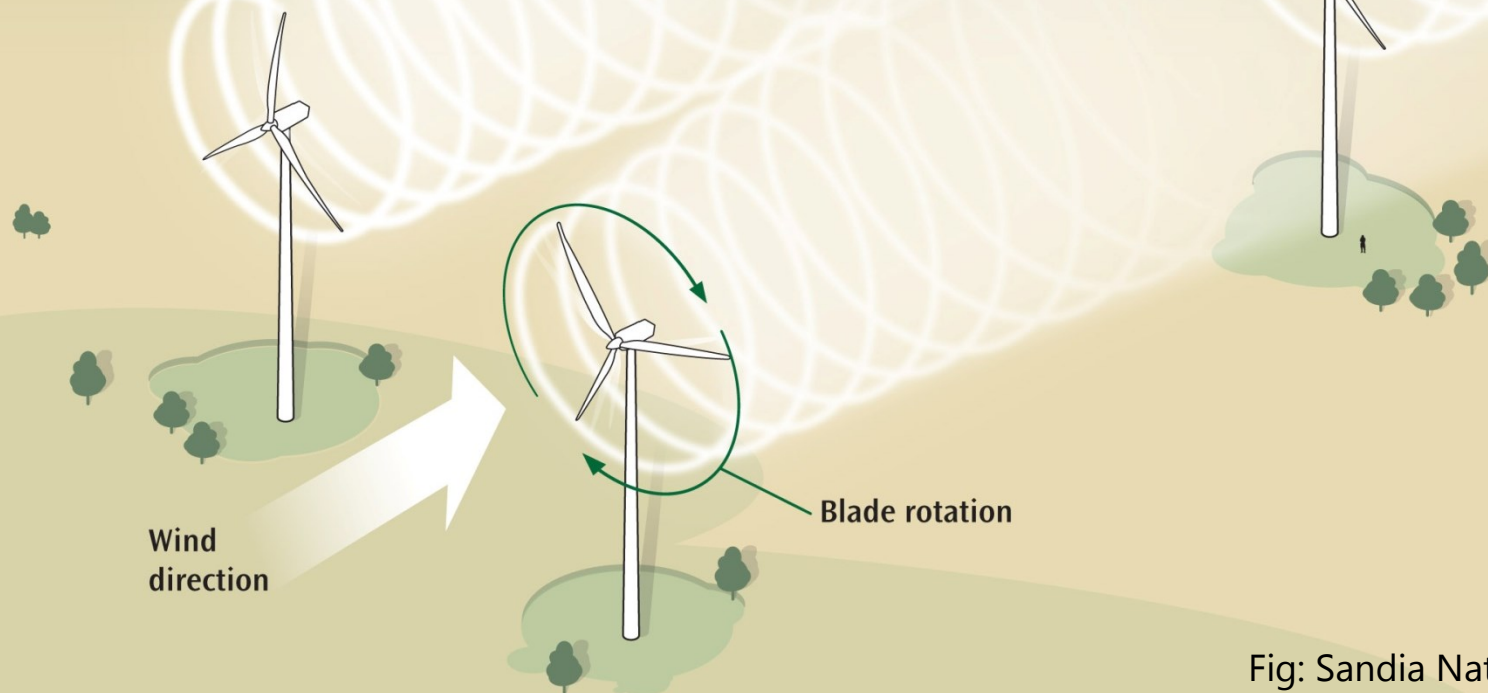
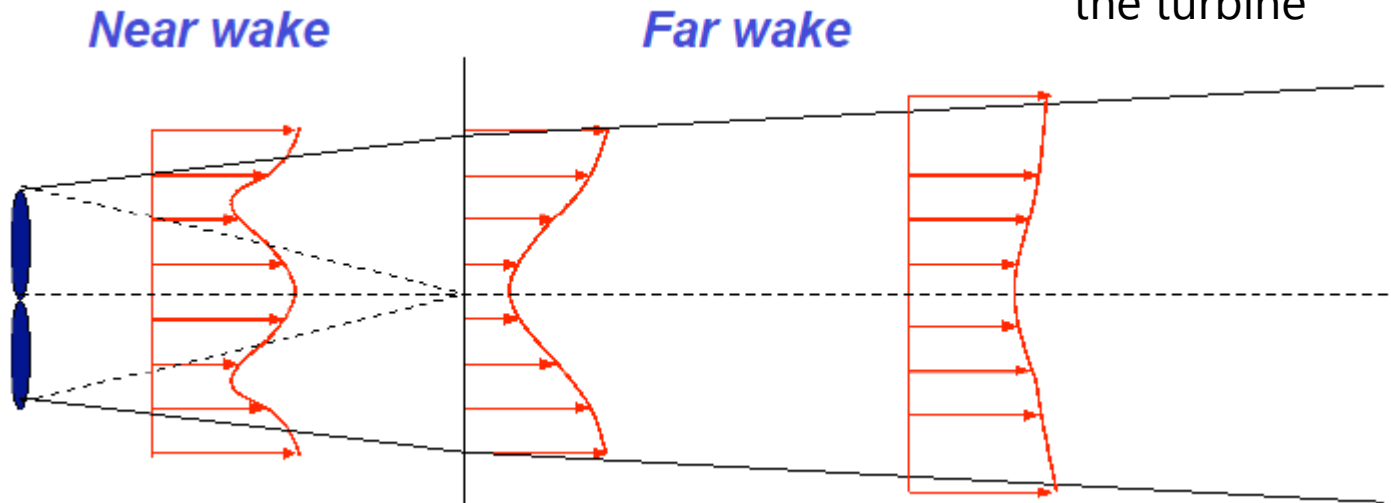


Fig: Sandia National Laboratory

# Velocity deficit profile in the near and far wake

turbulent mixing causes the two local minima to merge into a single global minimum

amplitude decreases and width increases with distance behind the turbine



no rigid definition, but near wake usually taken to extend a few rotor diameters behind turbine

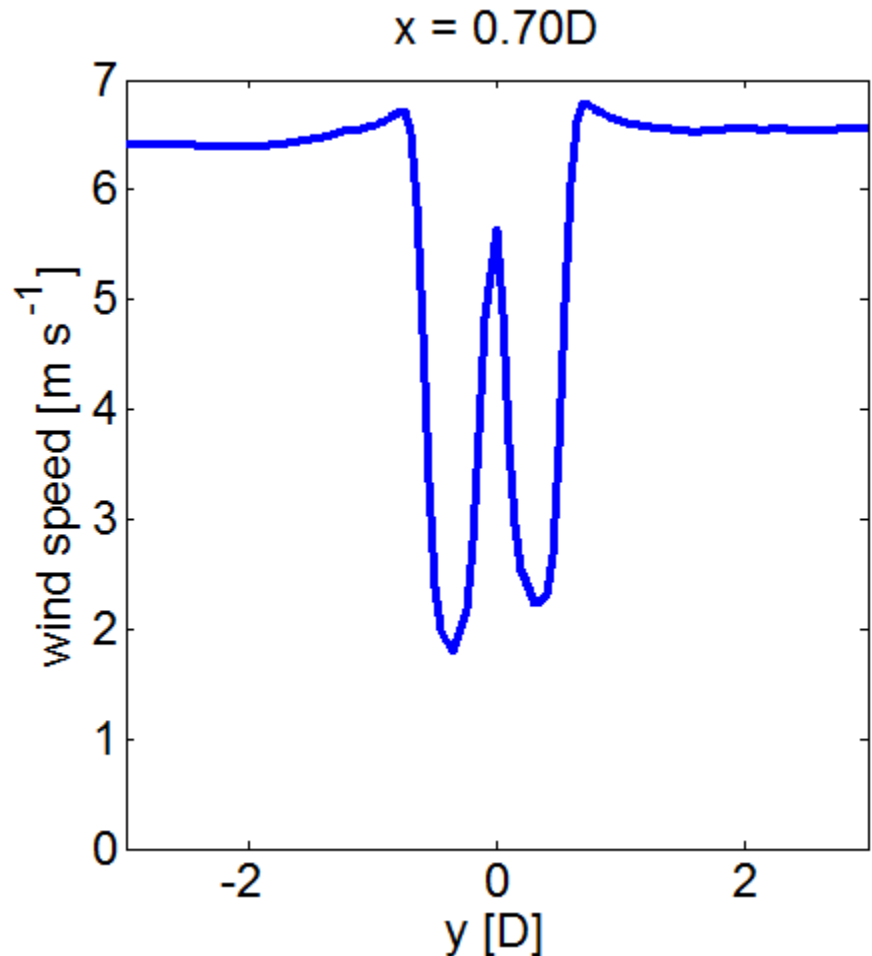
curve taken to be a Gaussian based on experimental evidence and similarity theory (Pope 2000)

# Velocity deficit profile as simulated by WRF

- Just behind the turbine, the wake expands initially b/c of mass conservation
  - profile has two local minima
- In the far wake, the velocity deficit decreases and the wake boundary increases with downstream distance
  - turbulent mixing causes the ambient flow to be entrained within the wake
  - profile has one global minimum

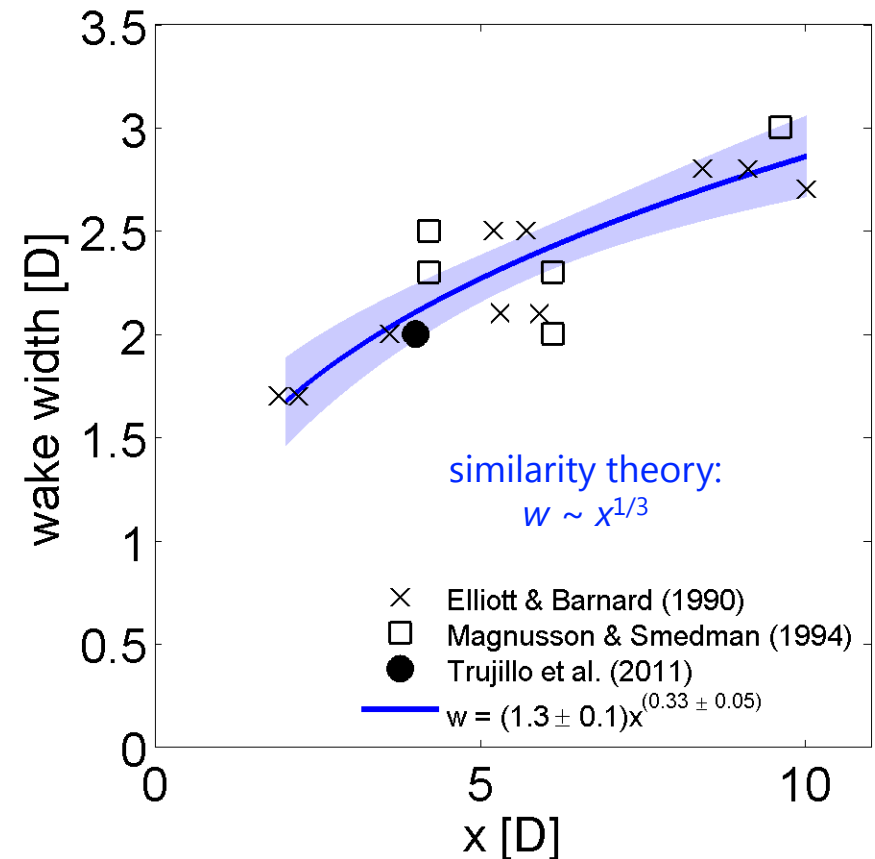
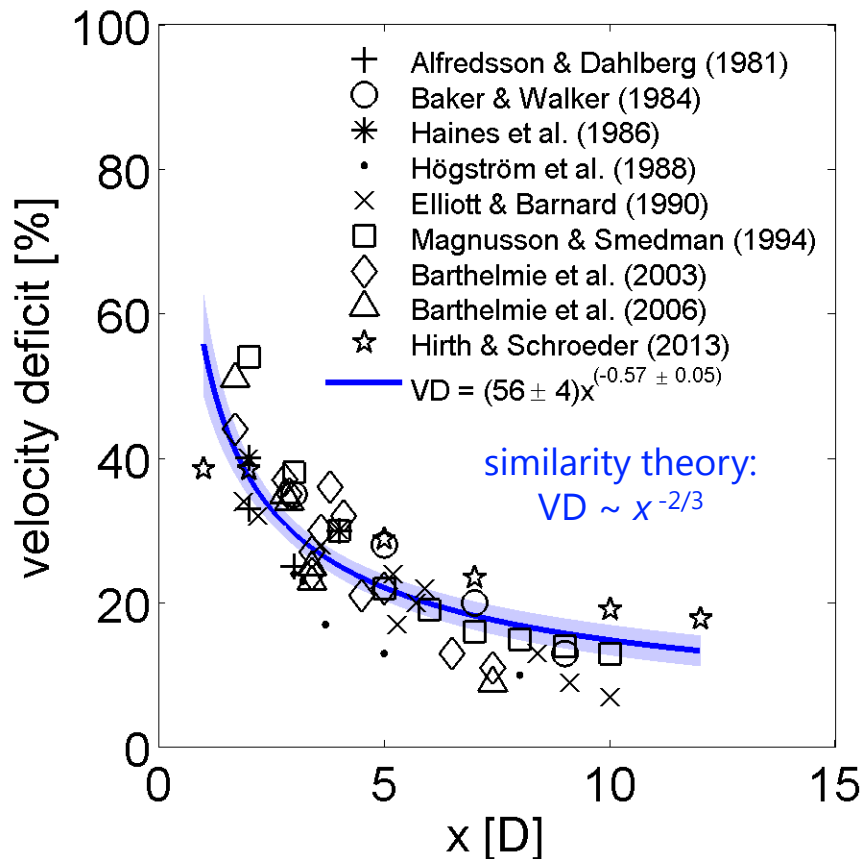
# Velocity deficit profile as simulated by WRF

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  - profile has one global minimum
- $x$  = downstream distance
- $D$  = rotor diameter

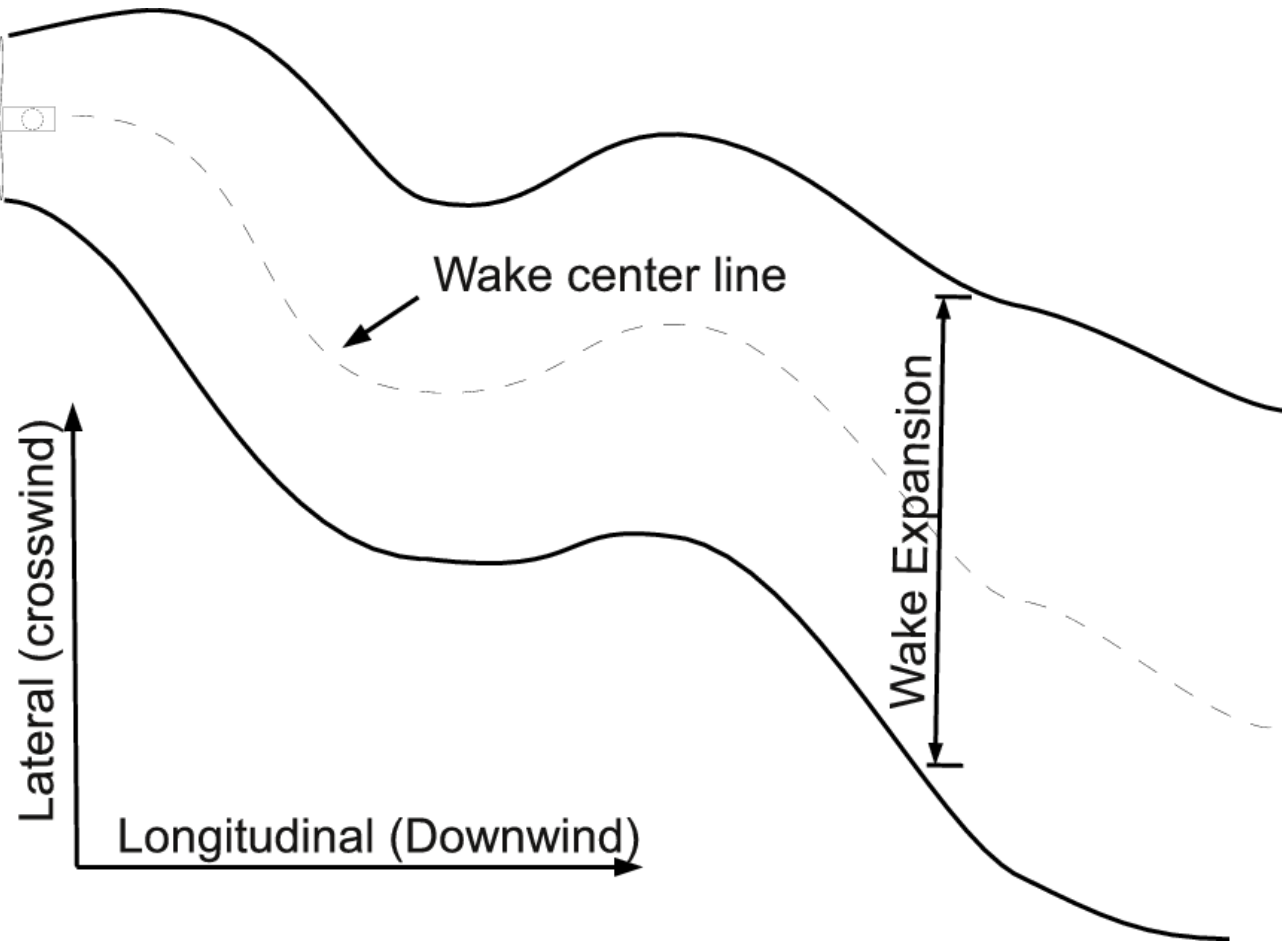


# Previous wake measurements made using met towers, sodar, UAS, lidar, and radar

$$VD = \frac{u_{\text{ambient}} - u_{\text{wake}}}{u_{\text{ambient}}} \times 100\%$$



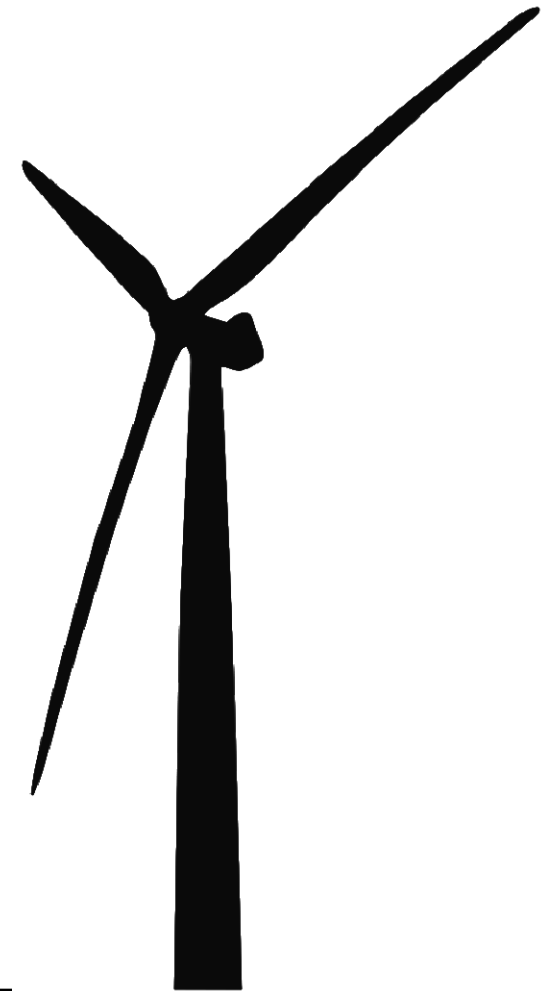
# Wake meandering driven by eddies with length scales on the order of the rotor





# Uncertainty in the literature as to the vertical location of the wake centerline

- Wake center located *above* →
  - Magnusson and Smedman (1994); Helmis et al. (1995)
- Wake center located *at* →
  - Elliott and Barnard (1990); Kambezidis et al. (1990)
- Wake center located *near* ?
- Wake center located *below* →
  - Crespo et al. (1988)



# Improving upon wake characterization from previous remote sensing experiments

- [Käsler et al. \(2010\)](#): first long-range lidar study, but very brief analysis limited to a single scan
- [Bingöl et al. \(2010\)](#) and [Trujillo et al. \(2011\)](#)
  - nacelle-mounted ZephIR lidar with max range of 200 m
  - stall-regulated 95-kW test turbine w/ 29-m hub and 19-m rotor diameter
  - analysis focuses on horizontal wake meandering and is limited to just 10-min
- [Hirth et al. \(2012\)](#) and [Hirth & Schroeder \(2013\)](#): dual-Doppler radar methodology and wake tracking algorithm not readily generalized for application to other datasets
  - does not incorporate wake expansion
  - focuses mostly on tracking horizontal position of wake centerline
  - analysis limited to 1-hr period during rainfall
- [Jungo et al. \(2013\)](#): focuses mostly on testing various lidar scanning strategies
  - limited analysis of a few scans lasting 11 min each

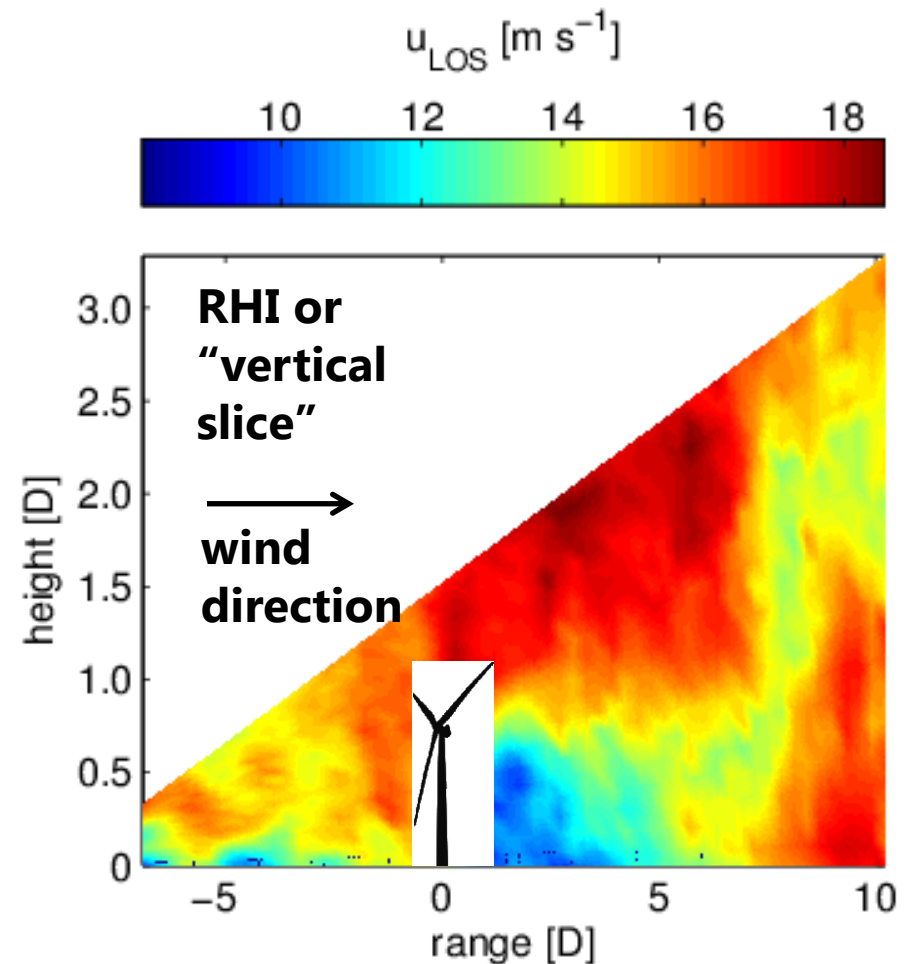
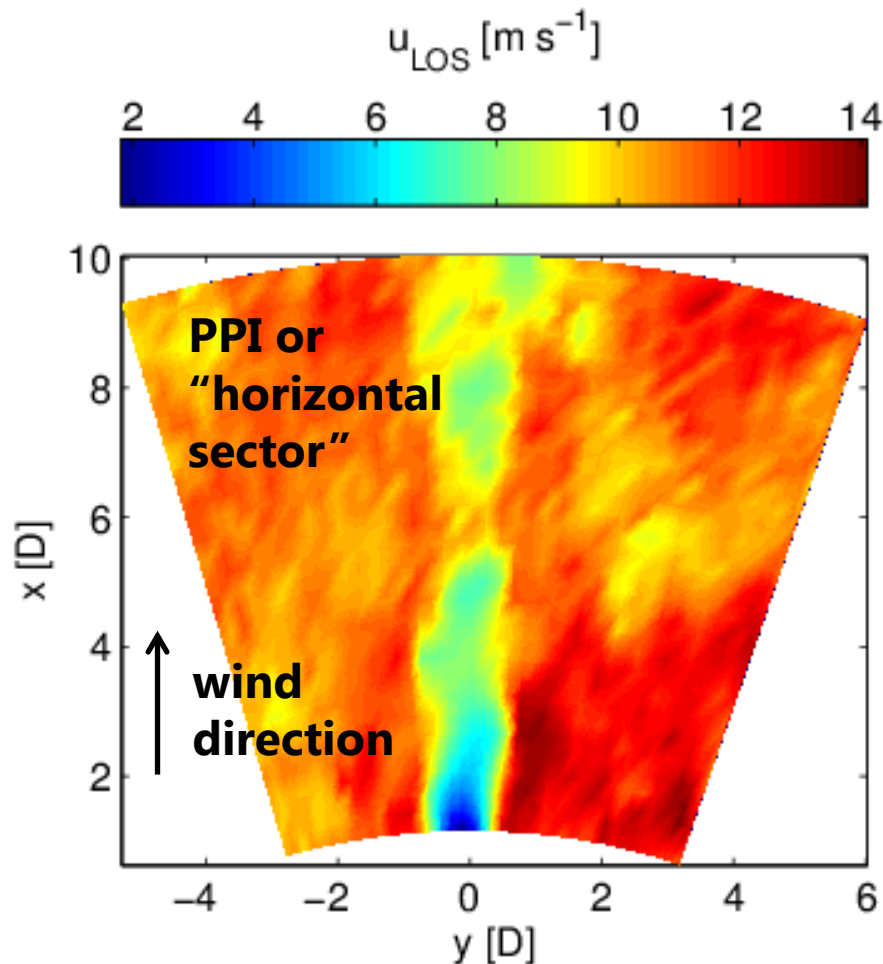
# Improving upon wake characterization from previous remote sensing experiments

- Need rigorous, general methodology for quantifying various wake characteristics
  - applicable to both remotely sensed measurements and numerical simulation output
- Need observations from modern pitch-regulated multi-MW turbines
- Need much more data to verify CFD models and to study effect of different atmospheric conditions
  - wind speed
  - turbulence
  - stability

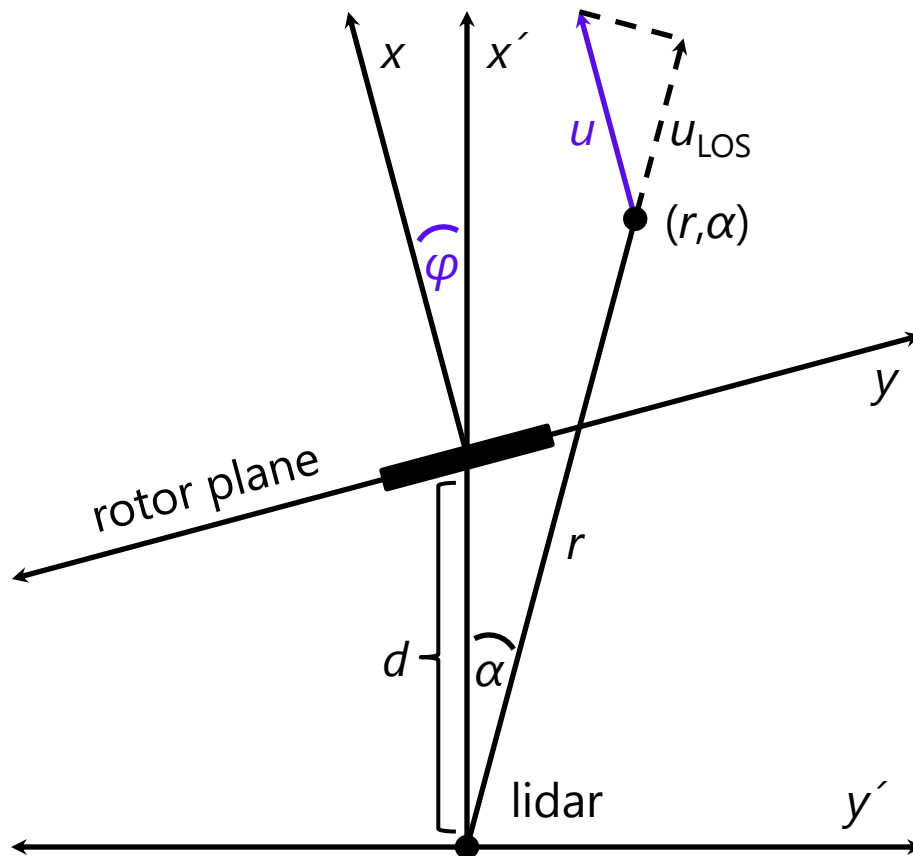
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# Lidar typically measures line-of-sight velocity ( $u_{\text{LOS}}$ ) using two scanning strategies



# Plan view of the coordinate systems with modeled parameters in purple



- $d$  = distance from lidar to turbine
- $r$  = lidar range gate
- $\alpha$  = lidar azimuth angle
- $u$  = ambient wind speed
- $\varphi$  = ambient wind direction
- $u_{\text{LOS}}$  = line-of-sight velocity measured by lidar

# Wake modeled as Gaussian function subtracted from uniform ambient flow

For each beam sweep, and at each range gate  $r$ , three models are fit to the lidar data to identify the wake, if any

Extra sum-of-squares F-test used to find simplest model to fit data

$$u_{\text{LOS}}(y', r) = u \cos(\alpha - \phi) = u \left( \frac{\sqrt{r^2 - y'^2}}{r} \cos \phi + \frac{y'}{r} \sin \phi \right)$$

ambient flow model

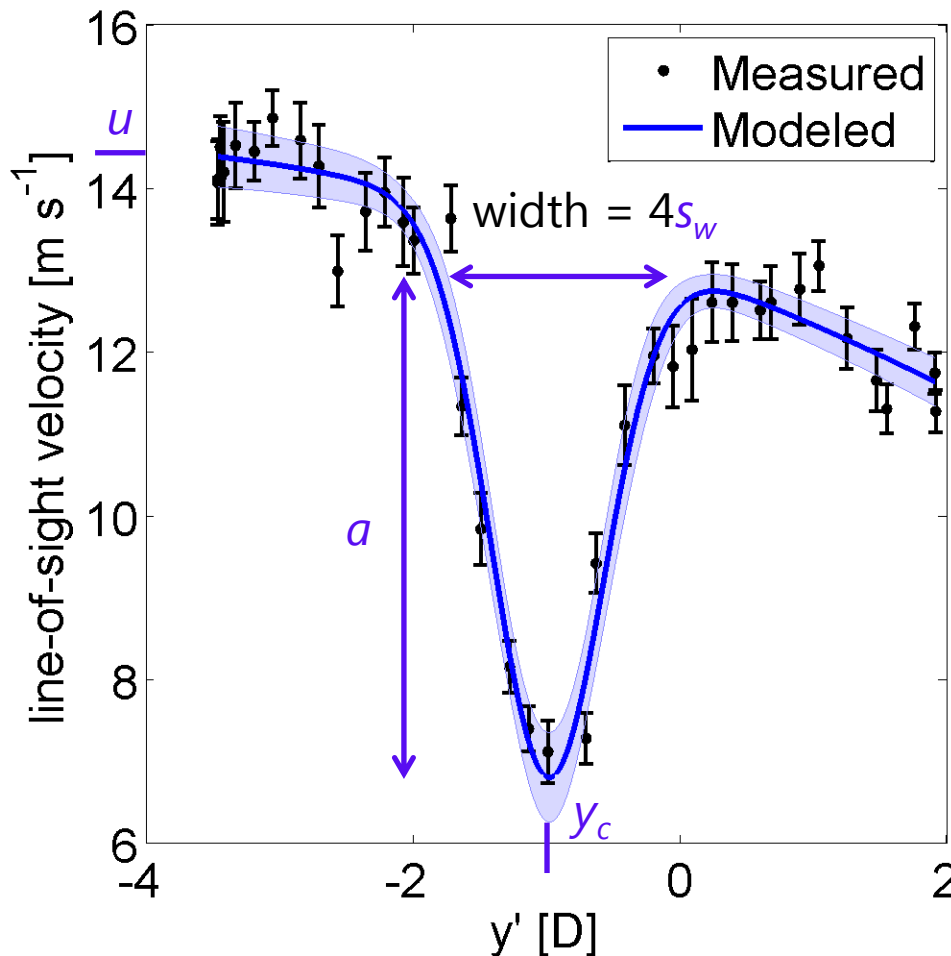
$$u_{\text{LOS}}(y', r) = \left( u - a \exp \left[ \frac{-(y' - y_c)^2}{2s_w^2} \right] \right) \left( \frac{\sqrt{r^2 - y'^2}}{r} \cos \phi + \frac{y'}{r} \sin \phi \right)$$

far wake model

$$u_{\text{LOS}}(y', r) = \left( u - a \left\{ \exp \left[ \frac{-(y' - y_l)^2}{2s_w^2} \right] + \exp \left[ \frac{-(y' - y_r)^2}{2s_w^2} \right] \right\} \right) \times \left( \frac{\sqrt{r^2 - y'^2}}{r} \cos \phi + \frac{y'}{r} \sin \phi \right)$$

near wake model

# Example fit to data from horizontal scan



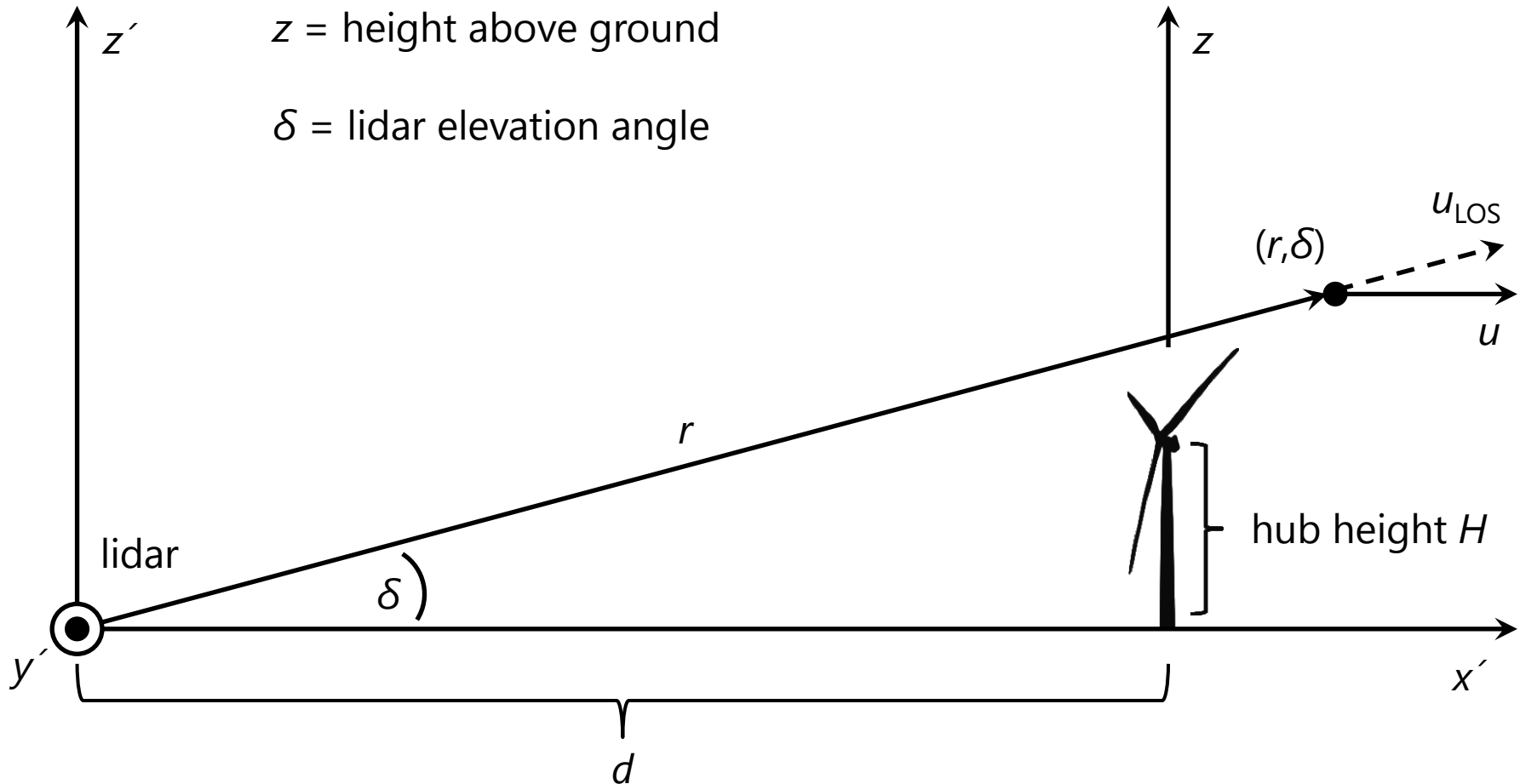
$y_c$ : algorithm capable of tracking wake meandering

wake width  $\equiv 4s_w$   
(Hansen et al. 2012)

$$\begin{aligned} \text{velocity deficit} &\equiv \frac{u_{\text{ambient}} - u_{\text{wake}}}{u_{\text{ambient}}} \times 100\% \\ &= \frac{u - (u - a)}{u} \times 100\% \\ &= \frac{a}{u} \times 100\% \end{aligned}$$



# Side view of the coordinate systems used for vertical scan model



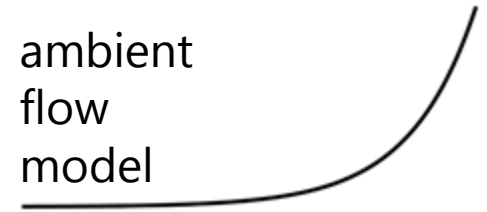
# Wake modeled as Gaussian subtracted from logarithmic wind speed profile

For each beam sweep, and at each range gate  $r$ , three models are fit to the lidar data to identify the wake, if any

Extra sum-of-squares F-test used to determine simplest model to fit data

$$u_{\text{LOS}}(z, r) = \frac{u_*}{k} \ln \left[ \frac{z}{z_0} \right] \cos \delta = \frac{u_*}{k} \ln \left[ \frac{z}{z_0} \right] \sqrt{1 - (z/r)^2}$$

ambient  
flow  
model



$$u_{\text{LOS}}(z, r) = \left( \frac{u_*}{k} \ln \left[ \frac{z}{z_0} \right] - a \exp \left[ \frac{-(z - z_c)^2}{2s_h^2} \right] \right) \sqrt{1 - (z/r)^2}$$

far  
wake  
model

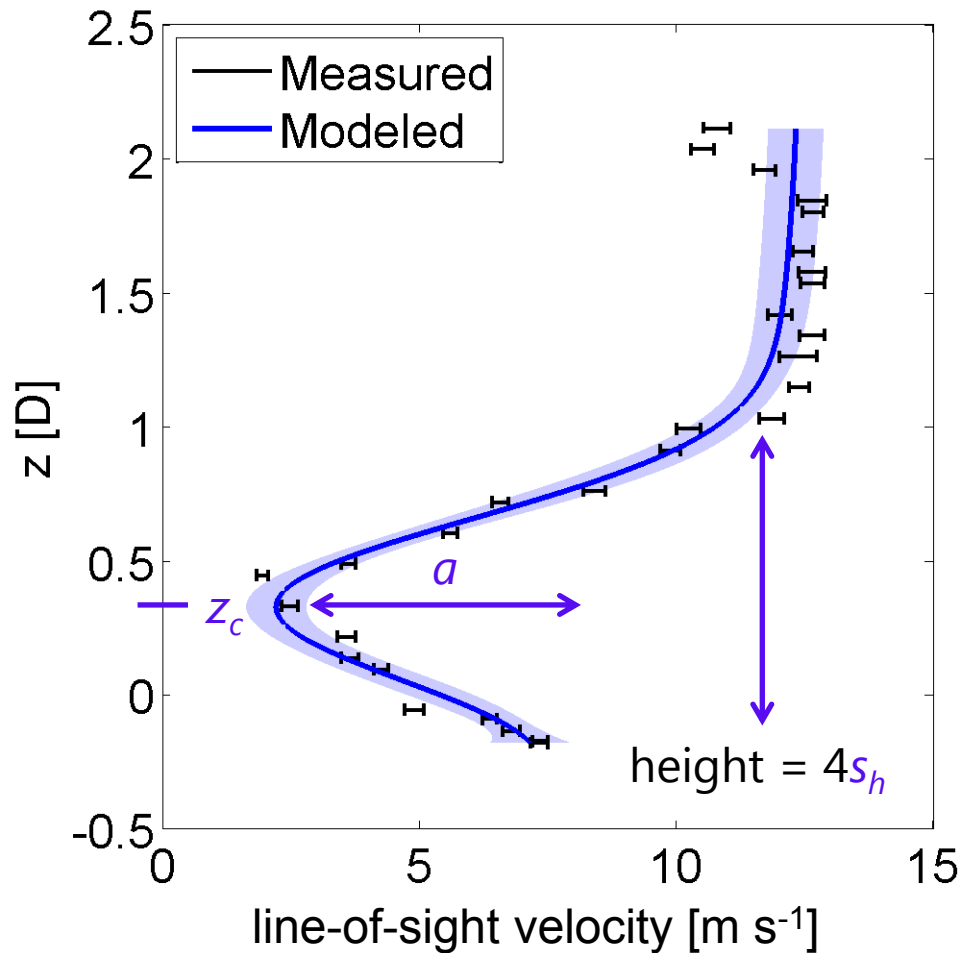


$$u_{\text{LOS}}(z, r) = \left( \frac{u_*}{k} \ln \left[ \frac{z}{z_0} \right] - a \left\{ \exp \left[ \frac{-(z - z_l)^2}{2s_h^2} \right] + \exp \left[ \frac{-(z - z_u)^2}{2s_h^2} \right] \right\} \right) \times \sqrt{1 - (z/r)^2}$$

near  
wake  
model



# Example fit to data from vertical scan



$z_c$ : algorithm capable of tracking vertical location of wake center

wake height  $\equiv 4s_h$   
(Hansen et al. 2012)

$$\text{velocity deficit} \equiv \frac{u_{\text{ambient}} - u_{\text{wake}}}{u_{\text{ambient}}} \times 100\%$$

$$u_{\text{ambient}} = \frac{u_*}{k} \ln \left[ \frac{z_c}{z_0} \right]$$

$$u_{\text{wake}} = u_{\text{ambient}} - a$$

# Outline

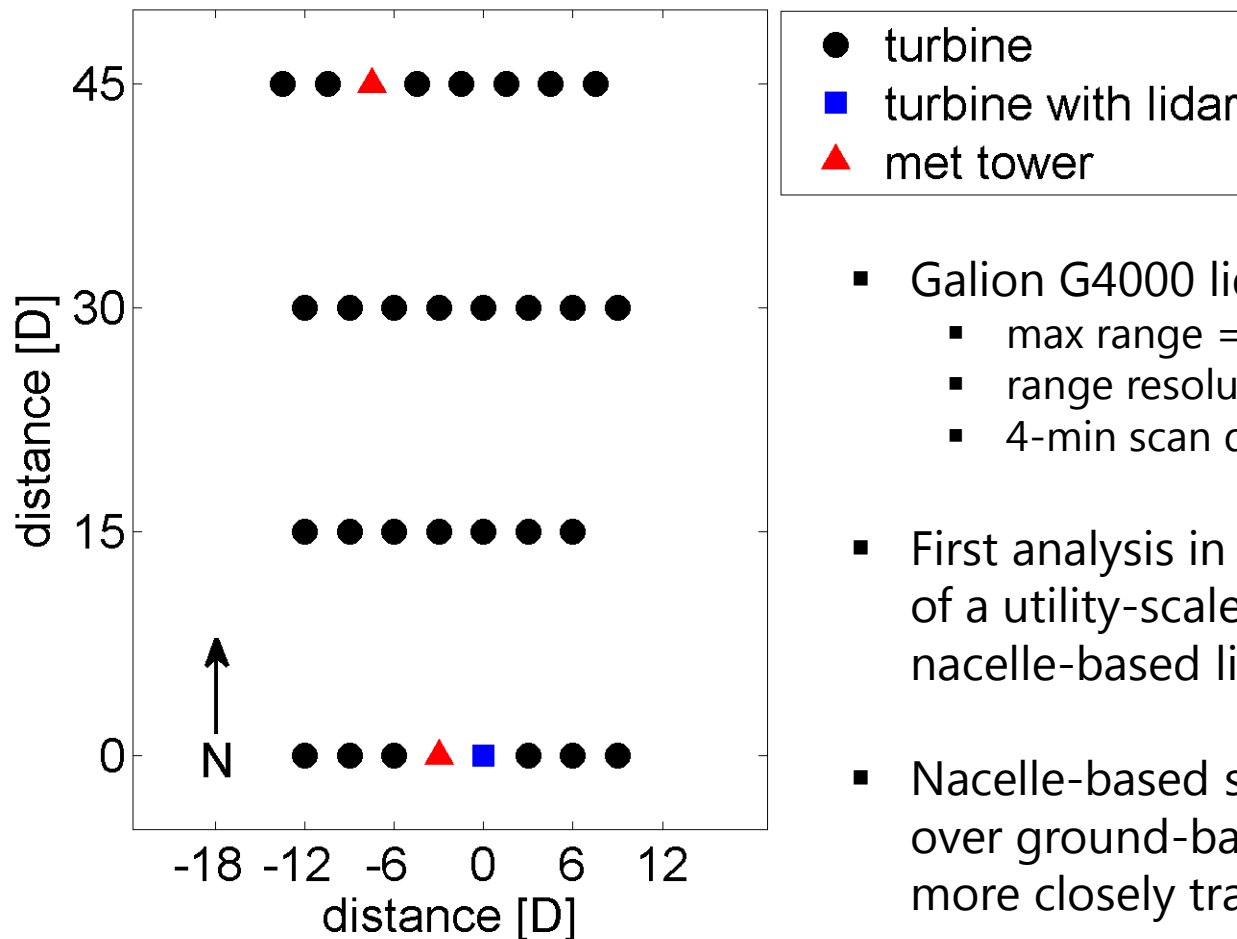
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# Lidar used to measure utility-scale turbine wakes in two experiments

	Experiment 1	Experiment 2
Location	National Wind Tech. Center	wind farm in western U.S.
Lidar type	ground-based   NOAA HRDL	nacelle-based   Galion G4000
Scan type	horizontal and vertical	horizontal
Data length	~100 hours	1 month
Reference	Aitken et al. (2014) <i>J. Atmos. Ocean. Tech.</i> , <b>31</b> , 765–787	Aitken/Lundquist (2014) <i>J. Atmos. Ocean. Tech.</i> , <b>31</b> , 1529–1539

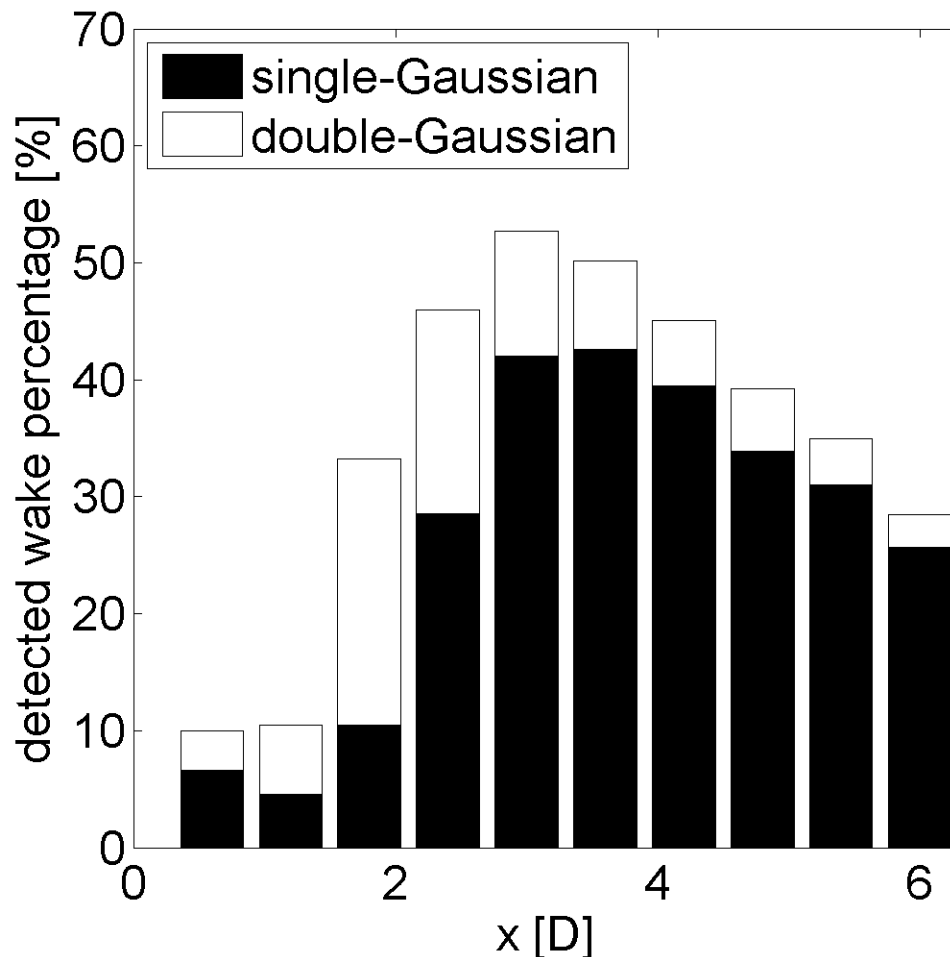


# Nacelle-based lidar experiment conducted at a wind farm in the western U.S.



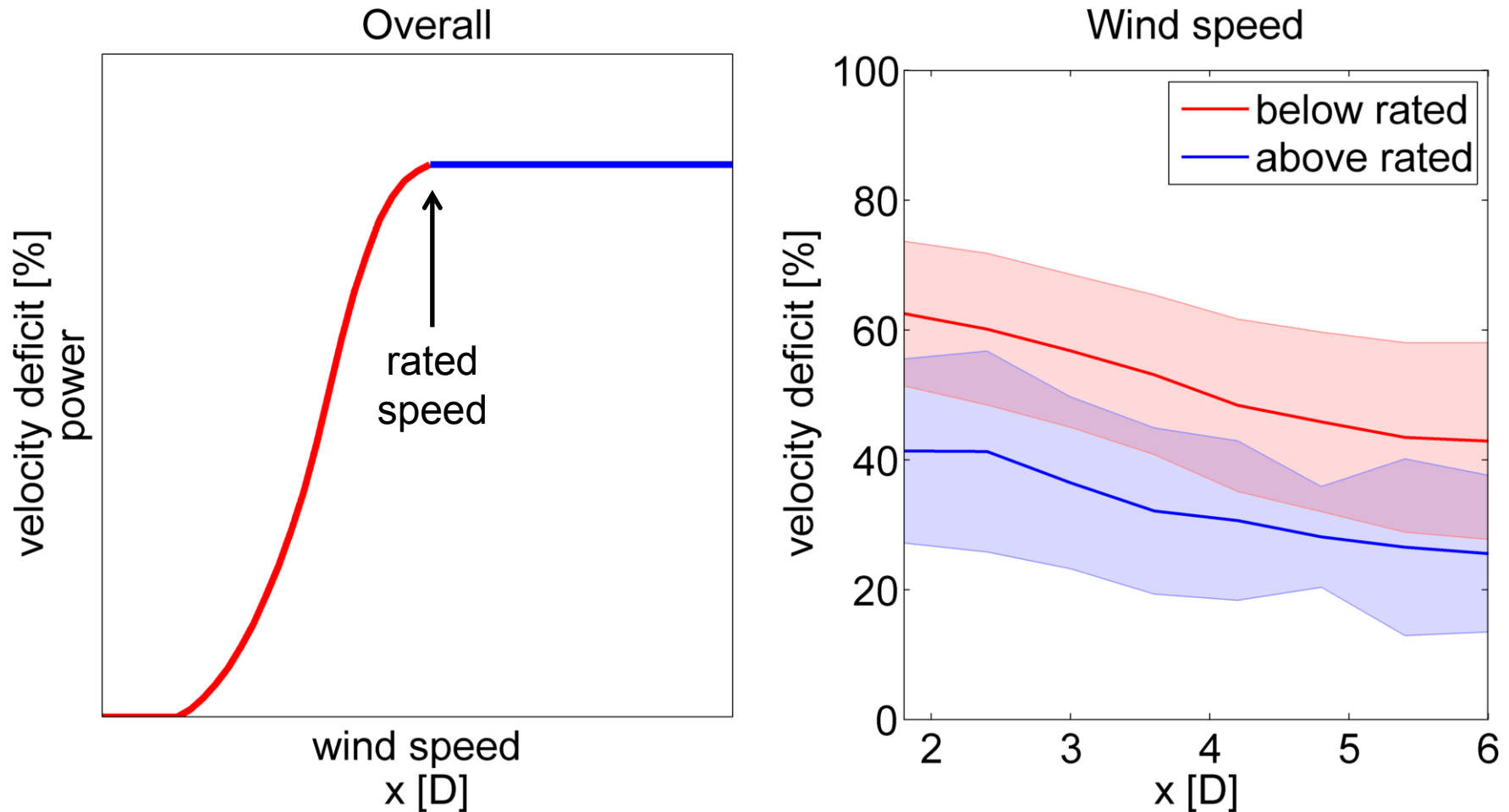
- Galion G4000 lidar
  - max range = 4 km
  - range resolution = 60 m
  - 4-min scan duration over 84° sector
- First analysis in the published literature of a utility-scale turbine wake using nacelle-based lidar
- Nacelle-based systems advantageous over ground-based ones b/c scans more closely transect wake centerline

# Wake detection rate



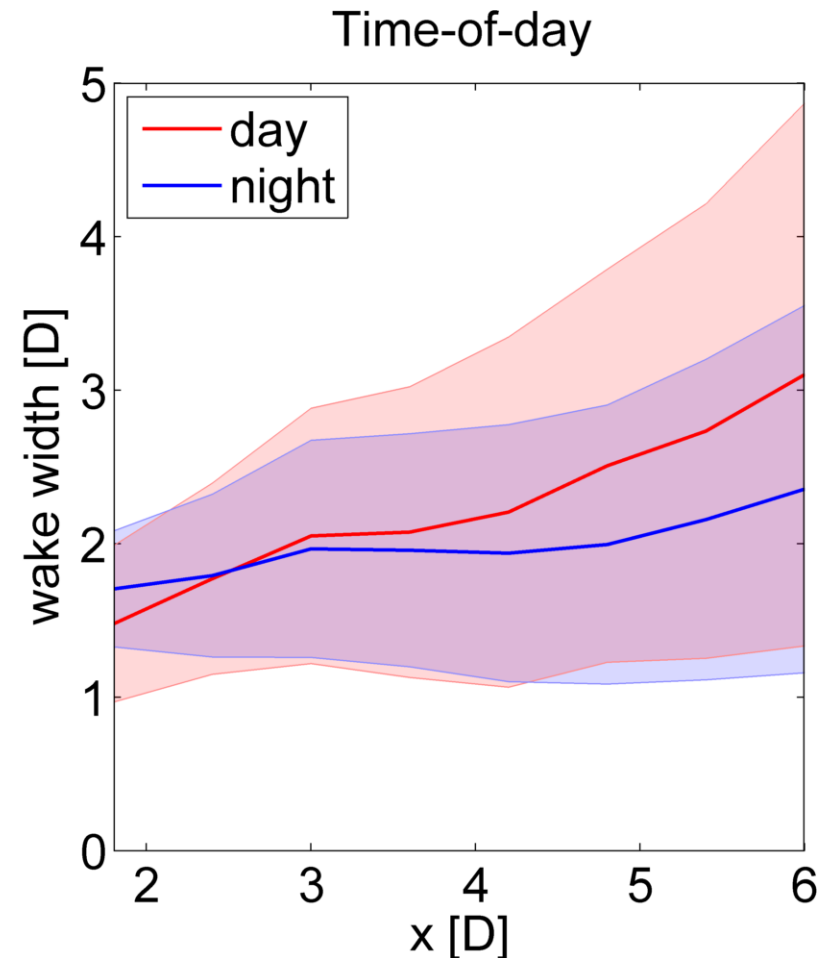
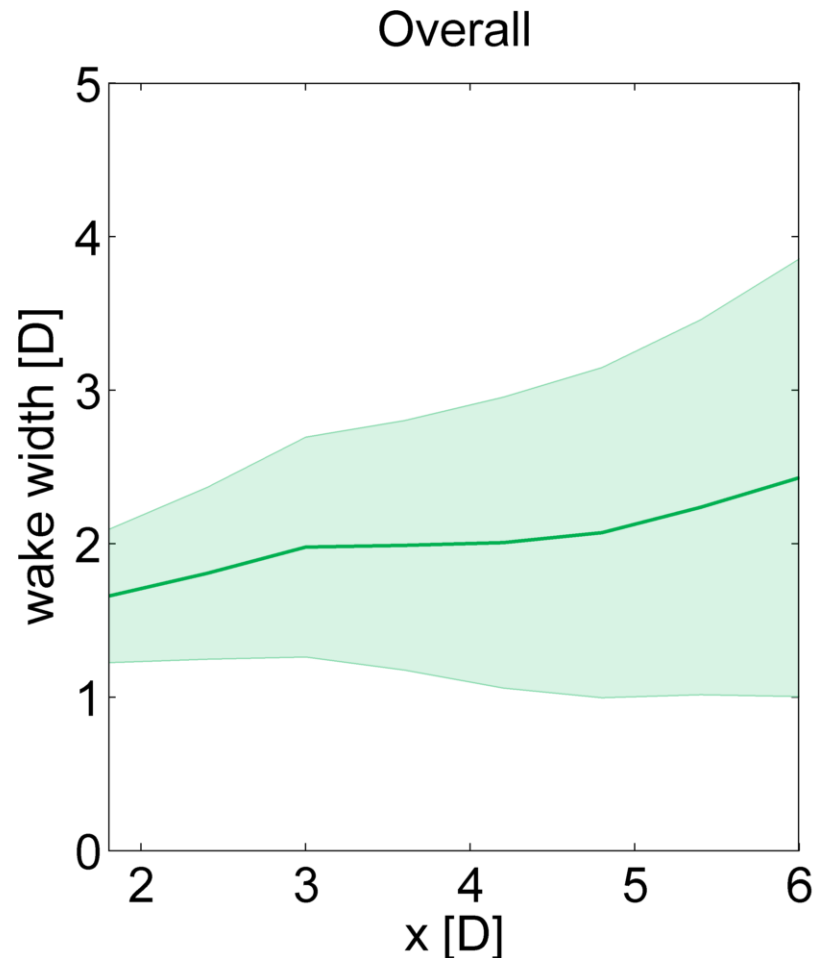
- Lidar field-of-view ( $84^\circ$  sector) not wide enough to capture wake near the turbine
  - need larger scan sector in future experiments
- Near wake lasts until  $\sim 3D$  downwind
- Wakes detected w/ diminishing frequency after  $x = 3D$ 
  - velocity deficit scales increasingly with ambient variability
  - velocity measurements are less precise at longer range gates
- Detection rate on par with España et al. (2011) *Wind Energy*, **14**, 923–937
  - particle image velocimetry in wind tunnel study

# Velocity deficit decreases with downstream distance because of turbulent mixing





# Wake boundary expands with downstream distance because of turbulent mixing



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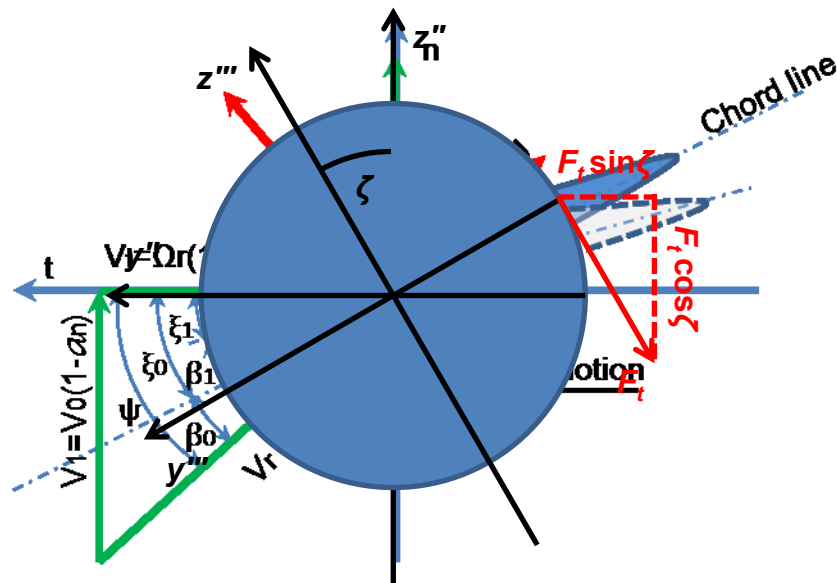
# Wind turbine performance depends on turbulence and atmospheric stability

- Rotating actuator disk model recently implemented in WRF-LES by Branko Kosović (NCAR) and Jeff Mirocha (LLNL)
  - comprehensive verification of this model requires simulating different turbines and atmospheric conditions

	Simulation 1	Simulation 2
Corresponding experiment	Experiment 1 (ground-based lidar @ NWTC)	Experiment 2 (nacelle-based lidar @ commercial wind farm)
Reference	Mirocha et al. (2014) <i>J. Renew. Sust. Energy</i> , <b>6</b> , 013104	Aitken et al. (2014) <i>J. Renew. Sust. Energy</i> , <b>6</b> , 033137
Stability	unstable	stable
Features	well-mixed surface heating convective cells thick boundary layer large characteristic eddies	wind shear surface cooling suppressed buoyancy shallow boundary layer small characteristic eddies

# Rotating actuator disk model in WRF-LES implemented by Kosović and Mirocha

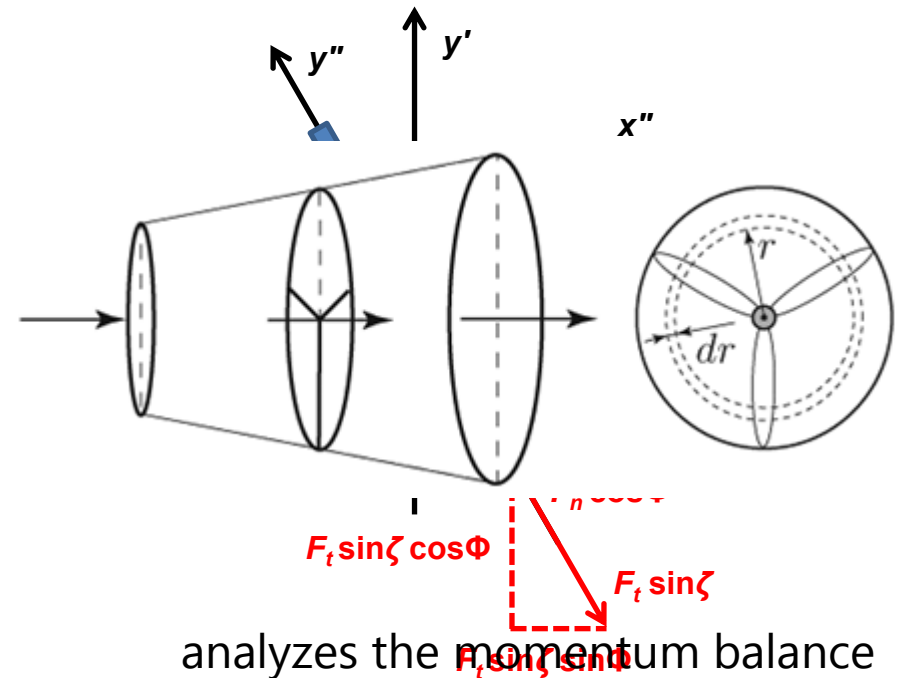
Blade Element Theory



calculates the lift and drag forces generated by the airfoil at various tangential forces along the blade

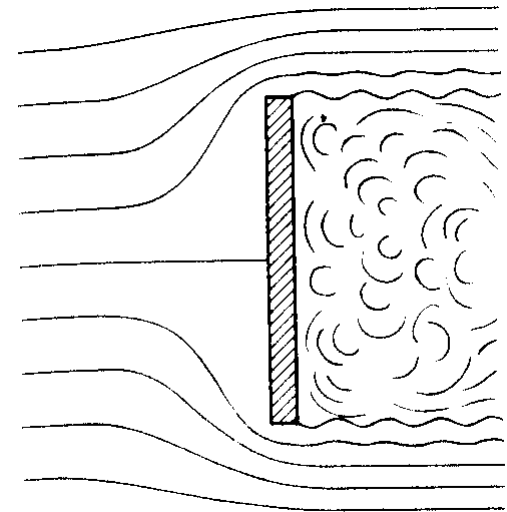
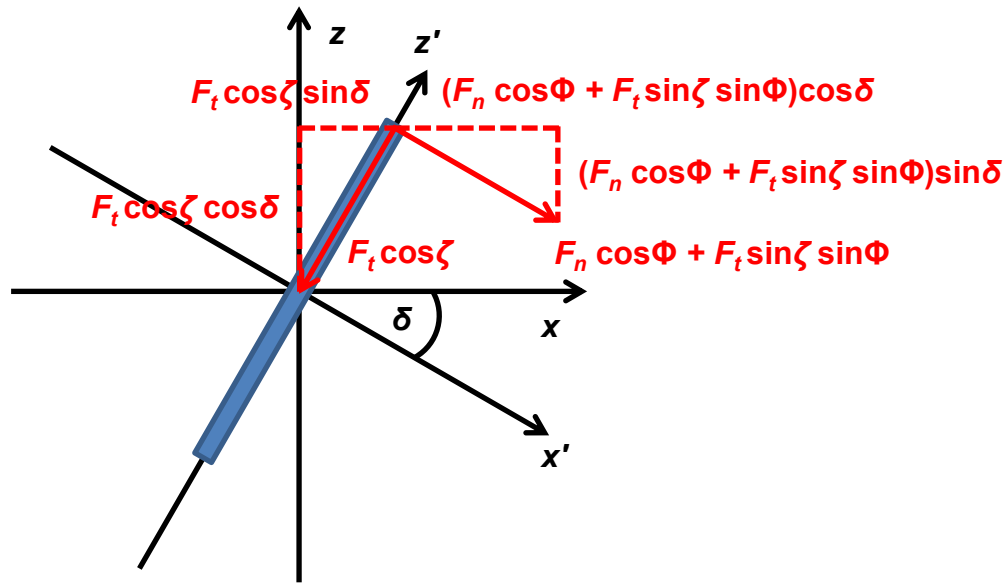
+

Momentum Theory



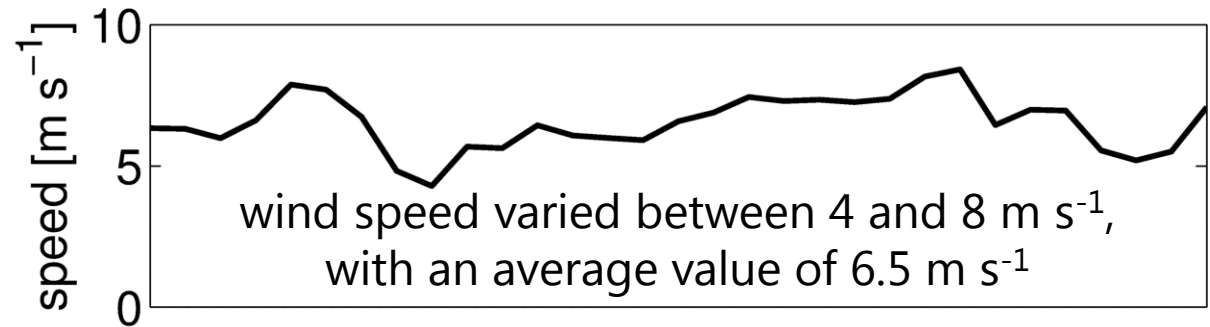
analyzes the momentum balance on a rotating annular stream tube passing through the turbine

# Modifications to actuator disk model: rotor tilt ( $\delta$ ) and drag from tower/nacelle

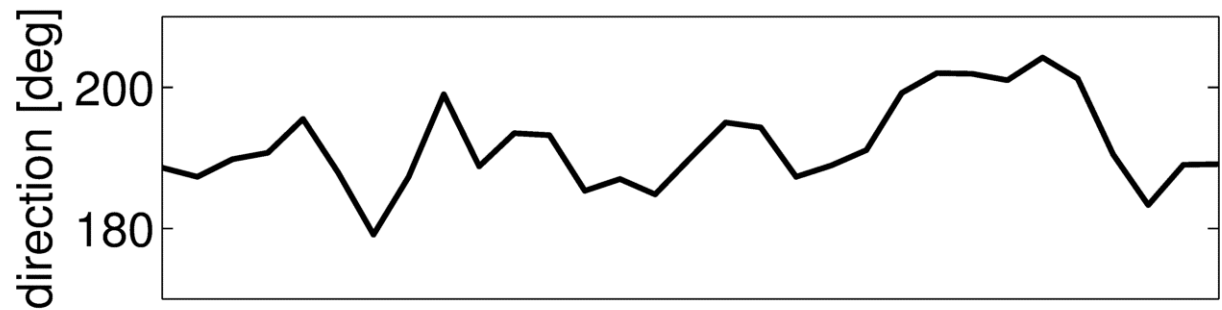


By Newton's third law, rotor tilt should cause the wake to be shifted upward

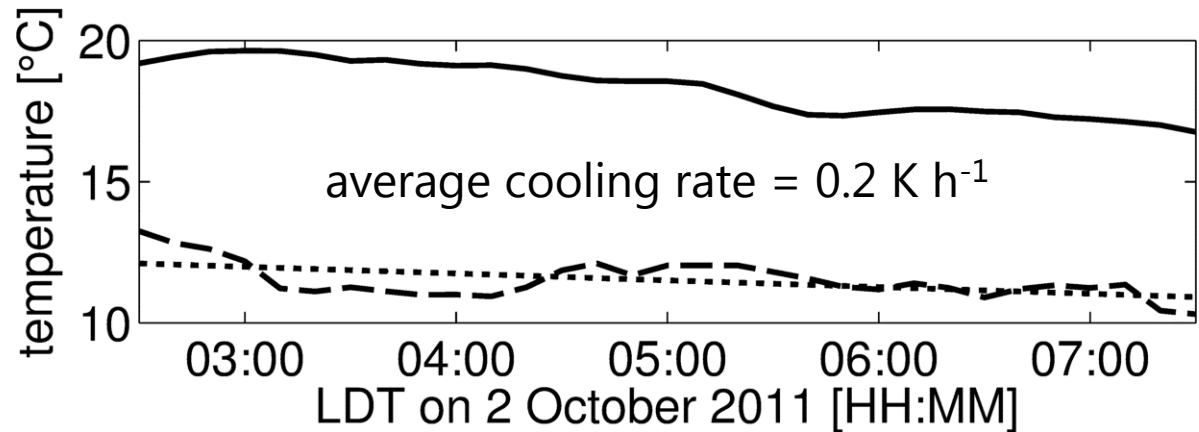
# Case study



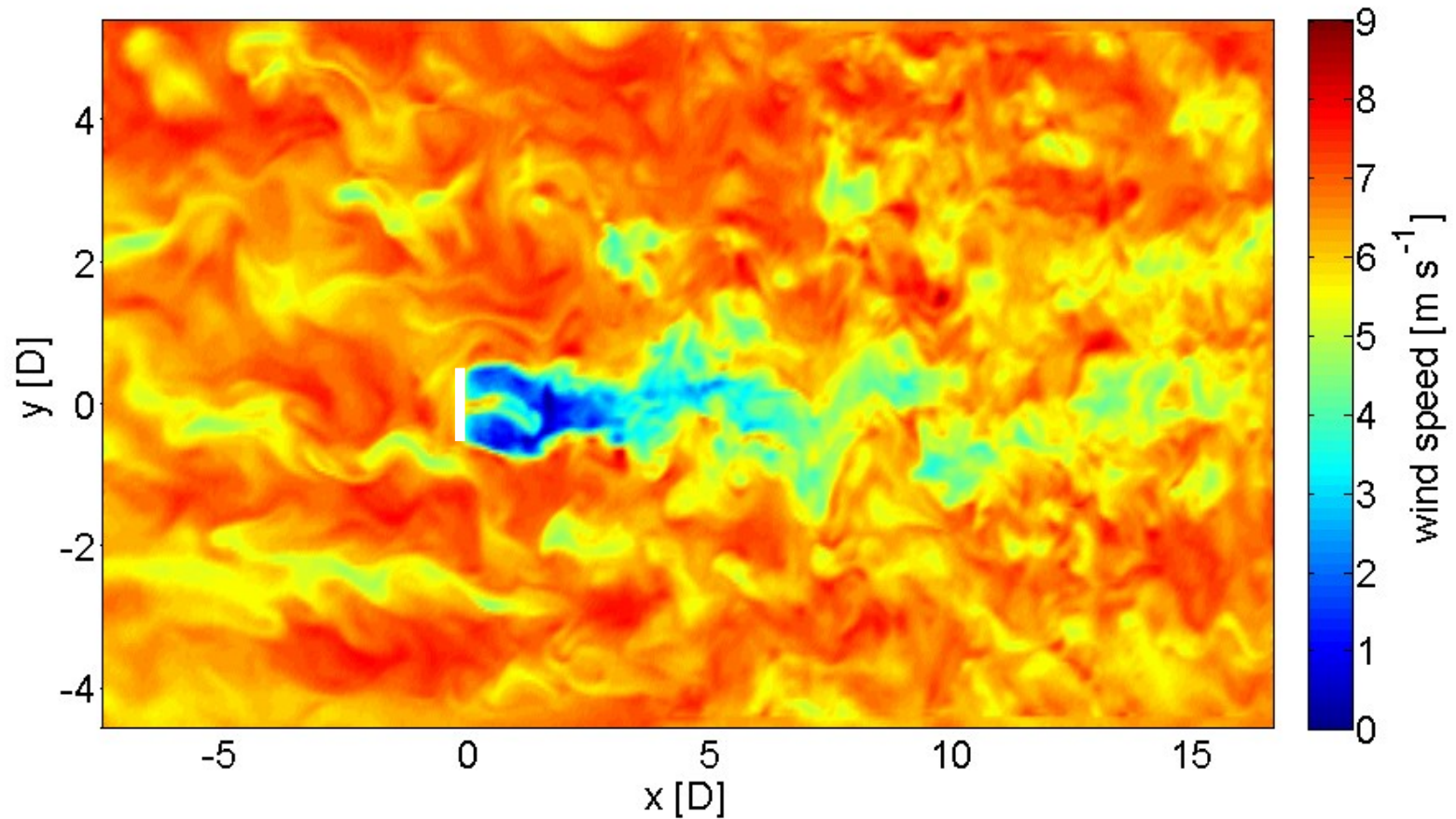
wind direction  
varied over a range  
of about 20 deg



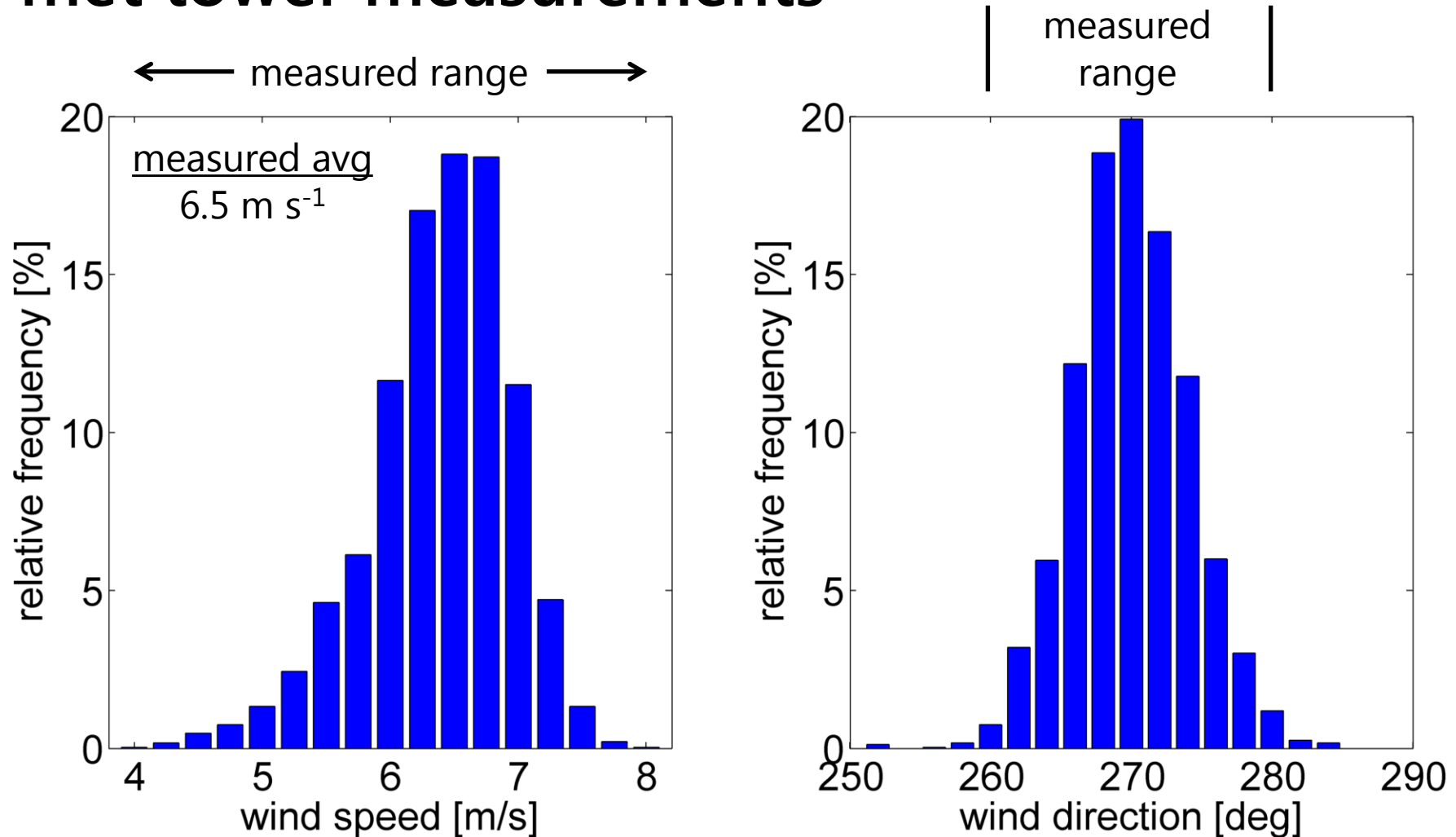
— hub height  
- - 2 m (measured)  
..... 2 m (linear fit)



# WRF simulation of wake dynamics

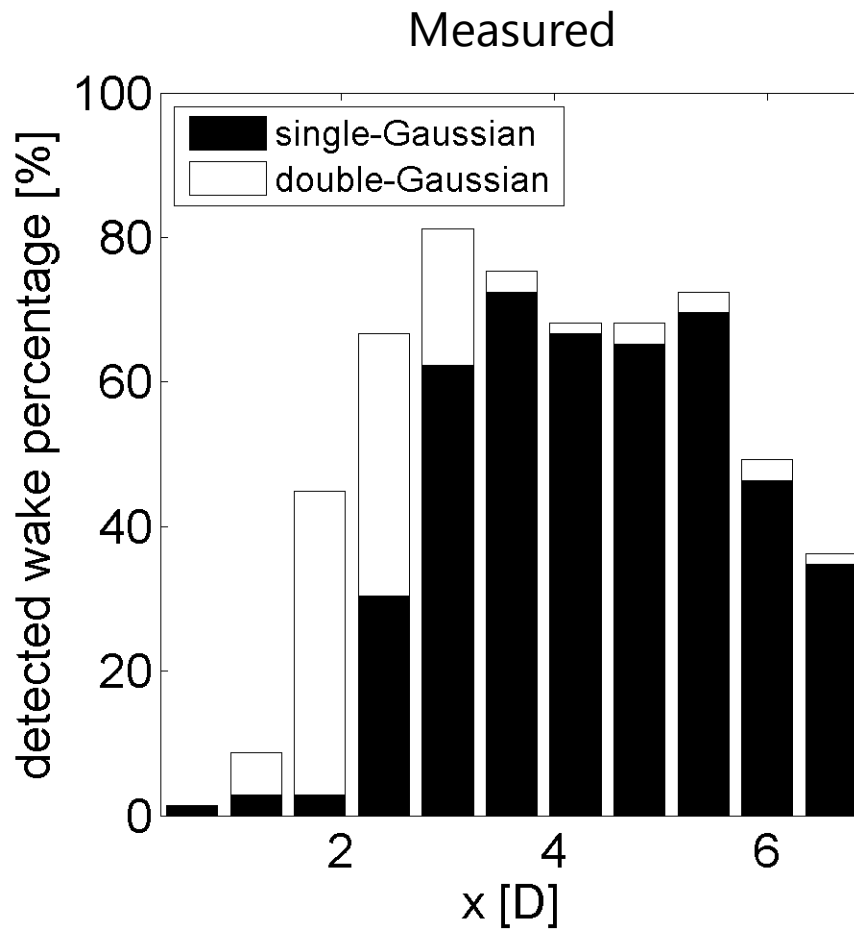


# Simulated inflow conditions closely match met tower measurements



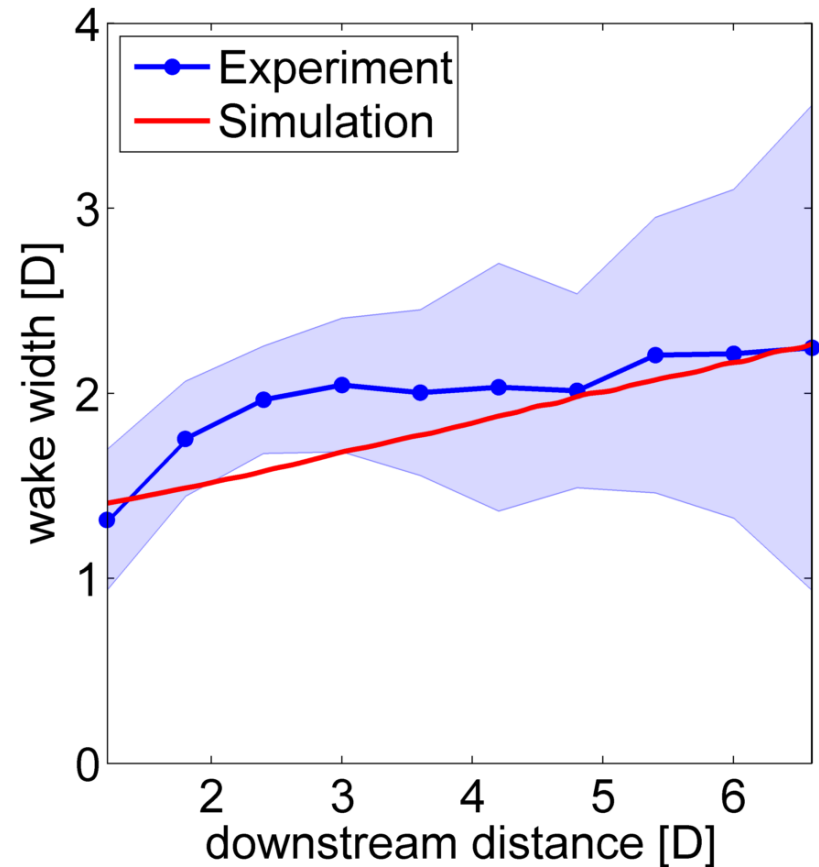
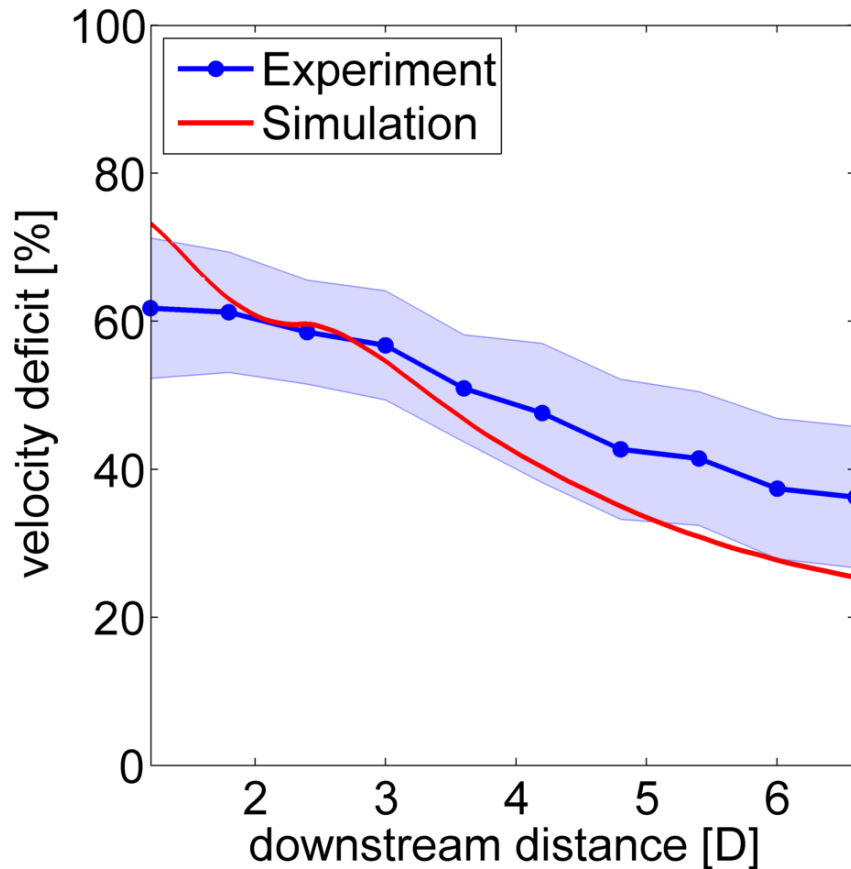


# Simulation is capable of representing the transition from the near to far wake



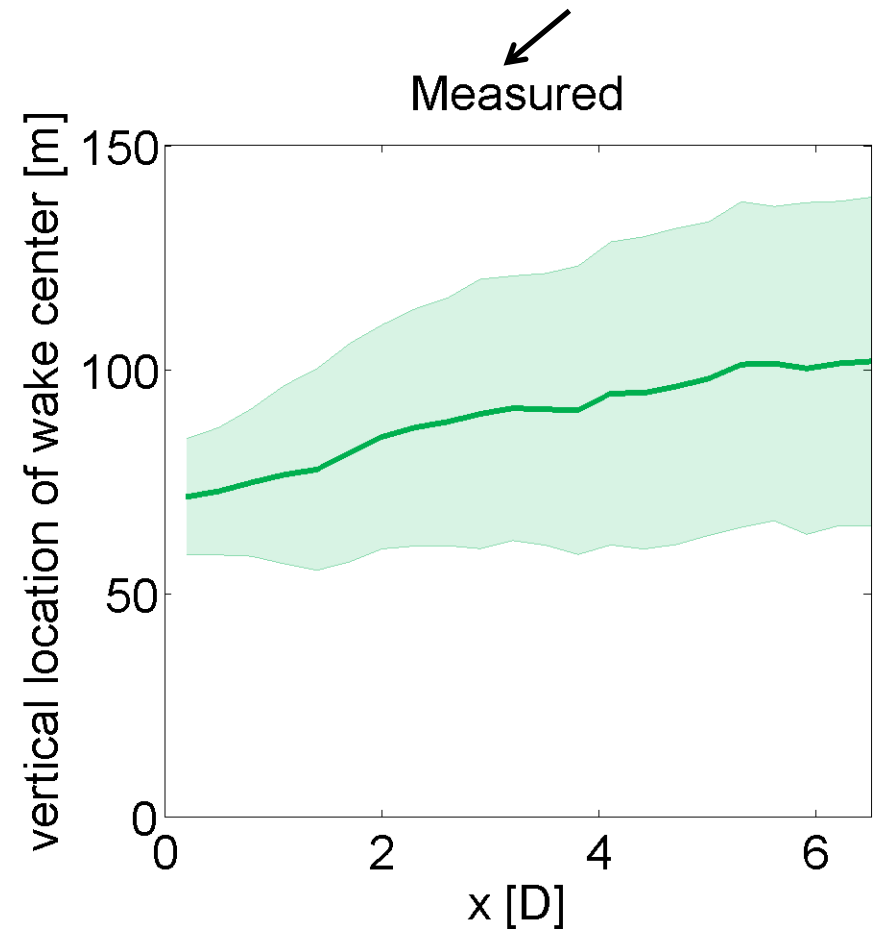
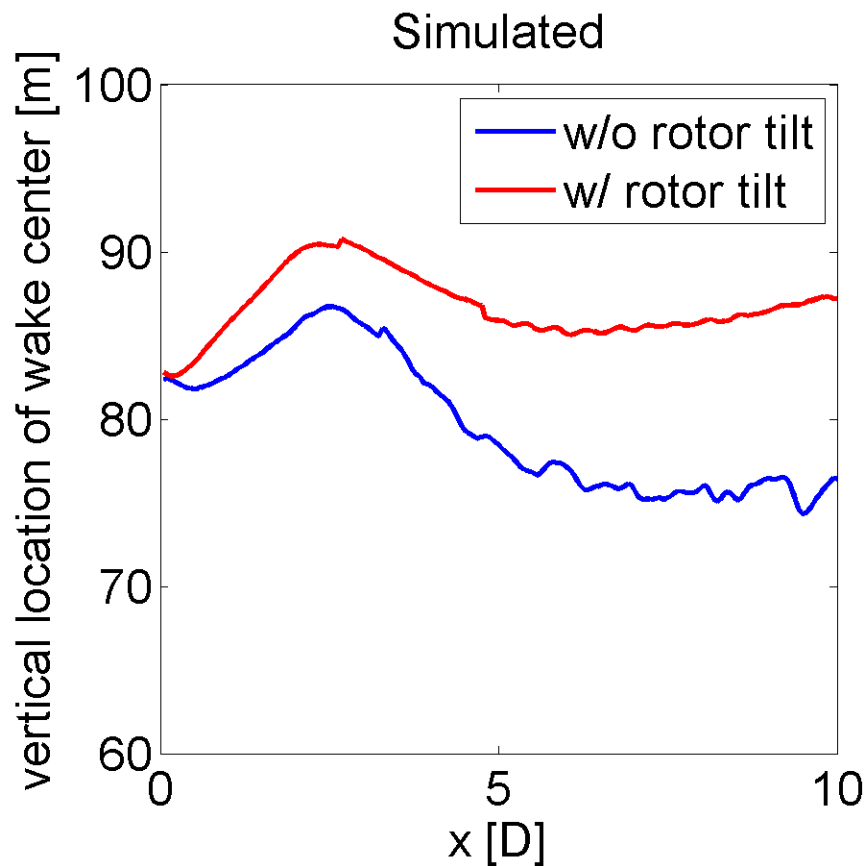
Simulated flow field transitions from a double-Gaussian to a single-Gaussian profile around  $x = 2-3D$

# Good agreement between measured and simulated results



# Vertical location of wake center is shifted upward because of rotor tilt

(analogous to results from Experiment 1)

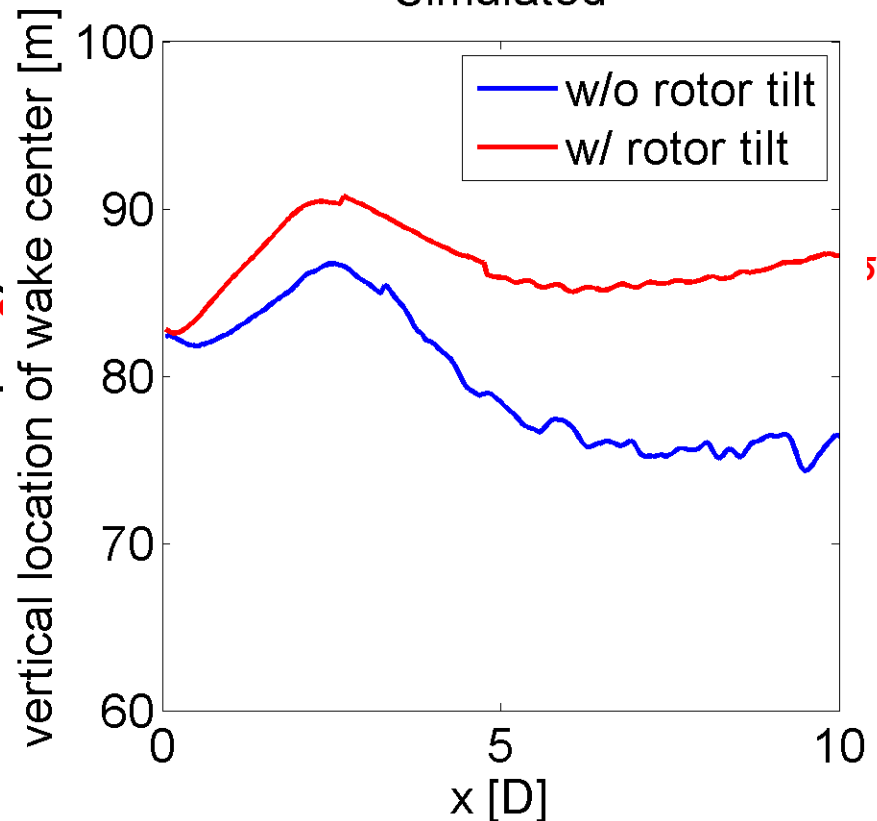
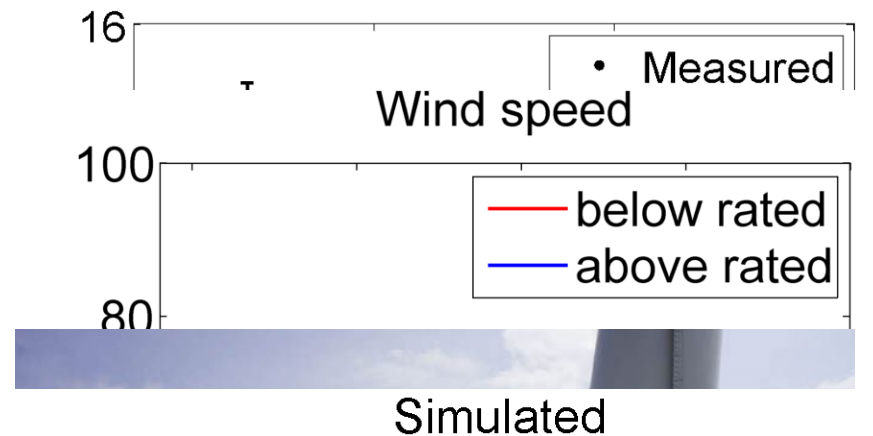


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- Developed statistical model for wind turbine wake characterization
  - generally applicable to experiment and simulation
  - allows for categorization of results by atmospheric conditions
- Conducted first analysis of utility-scale turbine wake using nacelle-based lidar
- Simulated stable conditions
- Added rotor tilt and tower/nacelle drag to actuator disk model in WRF-LES
  - demonstrated upward shift in wake centerline
- Good agreement between measured and simulated results



# Thank you



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